

```
:::::::::::::
makefile
:::::::::::::
.SUFFIXES : .o .cpp .c

.cpp.o :
    g++ -c -g -I$HOME/include $<

.c.o :
    g++ -c -g -I$HOME/include $<

OBS = cordic.o Angles.o Angles_tb.o          \
      Angles.1.plot_circle_angle.o         \
      Angles.2.plot_line_angle.o           \
      Angles.3.calc_statistics.o           \
      Angles.4.plot_statistics.o           \
      Angles.5.plot_residual_errors.o      \
      Angles.6.calc_uscale_statistics.o    \
      Angles.7.plot_uscale_statistics.o    \
      Angles.8.plot_uscale_residual_errors.o \
      Angles.9.plot_quantization.o        \

Angles.o : Angles.cpp Angles.hpp
    g++ -c -g -I$HOME/include Angles.cpp

Angles_tb : ${OBS}
    g++ -o $@ ${OBS} -lm

run : Angles_tb
    ./Angles_tb

QuadTree.o : QuadTree.cpp
    g++ -c -g -I$HOME/include QuadTree.cpp

QuadTree_tb.o : QuadTree_tb.cpp
    g++ -c -g -I$HOME/include QuadTree_tb.cpp

QuadTree_tb : QuadTree.o QuadTree_tb.o
    g++ QuadTree_tb.o QuadTree.o -o QuadTree_tb -lm

print :
    /bin/more makefile Angles.hpp cordic.hpp > print.file
    /bin/more ${OBS:o=cpp} >> print.file
    /bin/more QuadTree.hpp QuadTree.cpp QuadTree_tb.cpp > print.file2
    /bin/mv *.emf emf

clean :
    \rm -f *.o *~ *#
    \rm -f cordic_acc
    \rm -f cordic_ang
    \rm -f Angles_tb
    \rm -f *.emf

:::::::::::::
Angles.hpp
:::::::::::::
# include <iostream>
# include <iomanip>
# include <fstream>
```

```
# include <string>
// # include <cstdlib>
// # include <cmath>
# include <vector>
# include <algorithm>

using namespace std;

//-----
// Purpose:
//
// Class Angles Interface Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

//-----
// Compute Angles based on the binary tree
// idx - index for leaf nodes of the binary tree
// nIter - no of iteration (corresponds to the level of the tree)
//-----
double compute_angle ( int idx, int nIter );

//-----
// Draw Binary Angle Tree and Cumulative Binary Angle Tree
//-----
void draw_angle_tree (int nIter, int nAngle);

extern string GnuTerm;
const double pi = 3.141592653589793;
const double K = 1.646760258121;

class Angles
{
public:

Angles();
Angles(double *A, int nIter, int nAngle);

void setA(double *A);

void setNIter(int nIter);
void setNAngle(int nAngle);
void setThreshold(double threshold);

int getNIter();
```

```
int    getNAngle();
double getThreshold();

//-----
// Plot angle vectors on a unit circle
//-----
void plot_circle_angle ();

//-----
// Plot angle vectors on a linear scal
//-----
void plot_line_angle ();

// -----
// Find Angles Statistics --> member data
// -----
void calc_statistics ();

// -----
// Delta Distribution Plot and Angle-Delta Plot
// -----
void plot_statistics ();

//-----
// plot residual errors
// Residuals-Angle Plot and Residuals-Index Plot
//-----
void plot_residual_errors ();

void calc_uscale_statistics (double, double);
void plot_uscale_statistics ();
void plot_uscale_residual_errors ();
void plot_uscale_residual_errors (double, double);

//-----
// Plot Non-uniform Quantization of CORDIC
//-----
void plot_quantization ();
```

**private:**

```
double *A;
int    nIter;
int    nAngle;
int    Leaf;

double avg_delta;
double std_delta;
double min_delta;
double max_delta;
double min_angle;
double max_angle;

double ssr;    // sum of the squares of the residuals
double mse;    // mean squared error
double rms;    // root mean square error
double max_err; // maximum of squared errors

double threshold;
```

```
};
```

```

:::::::::::::
cordic.hpp
:::::::::::::
void cordic ( double *x, double *y, double *z, int n, int *, int, double =0.0 );
:::::::::::::
cordic.cpp
:::::::::::::
# include <cstdlib>
# include <iostream>
# include <iomanip>
# include <cmath>
# include <ctime>

using namespace std;

# include "cordic.hpp"

//*****80
void cordic ( double *x, double *y, double *z, int n,
             int *nBreak, int nBreakInit, double threshold)

//*****80
// CORDIC returns the sine and cosine using the CORDIC method.
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2012.04.17
//
// Author:
//
// Based on MATLAB code in a Wikipedia article.
//
// Modifications by John Burkardt
//
// Further modified by Young W. Lim
//
// Parameters:
//
// Input:
// *x: x coord of an init vector
// *y: y coord of an init vector
// *z: angle (-90 <= angle <= +90)
// n: number of iteration
// A value of 10 is low. Good accuracy is achieved
// with 20 or more iterations.
//
// Output:
// *xo: x coord of a final vector
// *yo: y coord of a final vector
// *zo: angle residue
//
// Local Parameters:
//
// Local, real ANGLES(60) = arctan ( (1/2)^(0:59) );
//
// Local, real KPROD(33), KPROD(j) = product ( 0 <= i <= j ) K(i),
// K(i) = 1 / sqrt ( 1 + (1/2)^(2i) ).
//
//
//
{

```

```
# define ANGLES_LENGTH 60
# define KPROD_LENGTH 33

double angle;
double angles[ANGLES_LENGTH] = {
  7.8539816339744830962E-01,
  4.6364760900080611621E-01,
  2.4497866312686415417E-01,
  1.2435499454676143503E-01,
  6.2418809995957348474E-02,
  3.1239833430268276254E-02,
  1.5623728620476830803E-02,
  7.81234106601011112965E-03,
  3.9062301319669718276E-03,
  1.9531225164788186851E-03,
  9.7656218955931943040E-04,
  4.8828121119489827547E-04,
  2.4414062014936176402E-04,
  1.2207031189367020424E-04,
  6.1035156174208775022E-05,
  3.0517578115526096862E-05,
  1.5258789061315762107E-05,
  7.6293945311019702634E-06,
  3.8146972656064962829E-06,
  1.9073486328101870354E-06,
  9.5367431640596087942E-07,
  4.7683715820308885993E-07,
  2.3841857910155798249E-07,
  1.1920928955078068531E-07,
  5.9604644775390554414E-08,
  2.9802322387695303677E-08,
  1.4901161193847655147E-08,
  7.4505805969238279871E-09,
  3.7252902984619140453E-09,
  1.8626451492309570291E-09,
  9.3132257461547851536E-10,
  4.6566128730773925778E-10,
  2.3283064365386962890E-10,
  1.1641532182693481445E-10,
  5.8207660913467407226E-11,
  2.9103830456733703613E-11,
  1.4551915228366851807E-11,
  7.2759576141834259033E-12,
  3.6379788070917129517E-12,
  1.8189894035458564758E-12,
  9.0949470177292823792E-13,
  4.5474735088646411896E-13,
  2.2737367544323205948E-13,
  1.1368683772161602974E-13,
  5.6843418860808014870E-14,
  2.8421709430404007435E-14,
  1.4210854715202003717E-14,
  7.1054273576010018587E-15,
  3.5527136788005009294E-15,
  1.7763568394002504647E-15,
  8.8817841970012523234E-16,
  4.4408920985006261617E-16,
  2.2204460492503130808E-16,
  1.1102230246251565404E-16,
  5.5511151231257827021E-17,
  2.7755575615628913511E-17,
  1.3877787807814456755E-17,
  6.9388939039072283776E-18,
  3.4694469519536141888E-18,
  1.7347234759768070944E-18 };
double c2;
double factor;
```

```
int j;
double kprod[KPROD_LENGTH] = {
    0.70710678118654752440,
    0.63245553203367586640,
    0.61357199107789634961,
    0.60883391251775242102,
    0.60764825625616820093,
    0.60735177014129595905,
    0.60727764409352599905,
    0.60725911229889273006,
    0.60725447933256232972,
    0.60725332108987516334,
    0.60725303152913433540,
    0.60725295913894481363,
    0.60725294104139716351,
    0.60725293651701023413,
    0.60725293538591350073,
    0.60725293510313931731,
    0.60725293503244577146,
    0.60725293501477238499,
    0.60725293501035403837,
    0.60725293500924945172,
    0.60725293500897330506,
    0.60725293500890426839,
    0.60725293500888700922,
    0.60725293500888269443,
    0.60725293500888161574,
    0.60725293500888134606,
    0.60725293500888127864,
    0.60725293500888126179,
    0.60725293500888125757,
    0.60725293500888125652,
    0.60725293500888125626,
    0.60725293500888125619,
    0.60725293500888125617 };
double pi = 3.141592653589793;
double poweroftwo;
double s2;
double sigma;
double sign_factor;
double theta;

double xn, yn;
```

```
//
// Initialize loop variables:
//
theta = *z;

xn = *x;
yn = *y;

poweroftwo = 1.0;
angle = angles[0];

angle = atan( 1. );

//
// Iterations
//
for ( j = 1; j <= n; j++ )
{
    if ( theta < 0.0 )
    {
        sigma = -1.0;
```

```

}
else
{
    sigma = 1.0;
}

//
// scaling factor is not yet corrected
//
static int cntBreak = 0;
if (nBreakInit == 0) cntBreak = 0;
if (abs(*z) < threshold) {
    *nBreak = ++cntBreak;

    // cout << "cntBreak= " << cntBreak;
    // cout << " z= " << *z;
    // cout << " < " << threshold << endl;
    break;
}

factor = sigma * poweroftwo;

*x =          xn - factor * yn;
*y = factor * xn +          yn;

xn = *x;
yn = *y;

//
// Update the remaining angle.
//
theta = theta - sigma * angle;

poweroftwo = poweroftwo / 2.0;

//
// Update the angle from table, or eventually by just dividing by two.
//
if ( ANGLES_LENGTH < j + 1 )
{
    angle = angle / 2.0;
}
else
{
    angle = angles[j];
}

angle = atan( 1. / (1 << j));

*z = theta;
}
//
// Adjust length of output vector to be [cos(beta), sin(beta)]
//
// KPROD is essentially constant after a certain point, so if N is
// large, just take the last available value.
//
// if ( 0 < n )
// {
//     *c = *c * kprod [ i4_min ( n, KPROD_LENGTH ) - 1 ];
//     *s = *s * kprod [ i4_min ( n, KPROD_LENGTH ) - 1 ];
// }
//
// Adjust for possible sign change because angle was originally
// not in quadrant 1 or 4.
//
// *c = sign_factor * *c;
// *s = sign_factor * *s;

```

```
    return;
# undef ANGLES_LENGTH
# undef KPROD_LENGTH
}
```

```
::::::::::::
Angles.cpp
```

```
::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"
# include "cordic.hpp"
```

```
using namespace std;
```

```
//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----
//
// double compute_angle ( int idx, int nIter )
// void draw_angle_tree (int nIter, int nAngle)
// Angles::Angles() : A(NULL), nIter(3), nAngle(8)
// void Angles::setNIter(int nIter)
// void Angles::setNAngle(int nAngle)
// void Angles::setThreshold(double th)
// int Angles::getNIter()
// int Angles::getNAngle()
// double Angles::getThreshold()
//
//-----
//
//-----
// Compute Angles based on the binary tree
// idx - index for leaf nodes of the binary tree
// nIter - no of iteration (corresponds to the level of the tree)
//-----
double compute_angle ( int idx, int nIter )
```



```

{
  double angle = 0.0;
  char s[32];
  int i, j;

  // i - bit position starting from lsb
  // j = 2^i
  // (idx & (1 << i)) - i-th bit of idx
  // if each bit is '1', add atan(1/2^i)
  // if each bit is '0', sub atan(1/2^i)
  // s[32] contains the binary representation of idx

  for (i=0; i<nIter; i++) {

    j = 1 << i;
    if (idx & (1 << i)) {
      angle += atan( 1. / j );
      s[nIter-i-1] = '1';
    } else {
      angle -= atan( 1. / j );
      s[nIter-i-1] = '0';
    }

    // cout << "i=" << i << " j=" << j << " 1/j=" << 1./j
    // << " atan(1/j)=" << atan(1./j)*180/3.1416 << endl;

  }
  s[nIter] = '\0';

  // cout << nIter << " " << idx << " " << s
  // << " ----> " << angle*180/3.1416 << endl;

  return angle;
}

//-----
// Draw Binary Angle Tree and Cumulative Binary Angle Tree
//-----
void draw_angle_tree (int nIter, int nAngle)
{
  int level = nIter;
  int i, j, k;
  ofstream myout;
  double *A;

  if (nIter > 10) {
    cout << "nIter = " << nIter << " is too large to plot! " << endl;
    return;
  }

  // cout << "nIter = " << nIter << endl;
  // cout << "nAngle = " << nAngle << endl;

  A = (double *) malloc(nAngle * sizeof (double));

  //-----
  // Binary Angle Tree
  //-----

  myout.open("angle.dat");

```

```

for (i=0; i<level; ++i) {
    nIter = i;
    nAngle = 1 << nIter;

    for (j=0; j<nAngle; ++j) {
        A[j] = compute_angle(j, nIter);

        // cout << "A[" << j << "] = " << A[j] << endl;
        myout << A[j]*180/pi << " " << i << " 0.0 1.0" << endl;
    }
}

myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
myout << "set output 'eg01.bin_ang_tree.emf'" << endl;
myout << "set title \"Binary Angle Tree\" " << endl;
myout << "set xlabel \"Angles in degree\" " << endl;
myout << "set ylabel \"Levels \" " << endl;
myout << "set format x \"%.0f\" " << endl;
myout << "set format y \"%.0f\" " << endl;
myout << "plot 'angle.dat' using 1:2:3:4 ";
myout << "with vectors head filled lt 3" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

//-----
// Cumulative Angle Tree
//-----

myout.open("angle.dat");

for (i=0; i<level; ++i) {

    for (k=0; k<=i; k++) {
        nIter = k;
        nAngle = 1 << nIter;

        for (j=0; j<nAngle; ++j) {
            A[j] = compute_angle(j, nIter);

            //cout << "A[" << j << "] = " << A[j] << endl;
            myout << A[j]*180/pi << " " << i << " 0.0 1.0" << endl;
        }
    }
}

myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
myout << "set output 'eg02.cumul_ang_tree.emf'" << endl;
myout << "set title \"Cumulative Binary Angle Tree\" " << endl;
myout << "set xlabel \"Angles in degree\" " << endl;
myout << "set ylabel \"Levels \" " << endl;
myout << "set format x \"%.0f\" " << endl;
myout << "set format y \"%.0f\" " << endl;
myout << "plot 'angle.dat' using 1:2:3:4 ";

```

```

myout << "with vectors head filled lt 4" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

free (A);
return;
}

//-----
// Class Angles' Member Functions
//-----
Angles::Angles() : A(NULL), nIter(3), nAngle(8)
{
    Leaf = 1;

    cout << "A is not initialized " << endl;
    cout << "nIter = " << nIter << endl;
    cout << "nAngle = " << nAngle << endl;

    avg_delta = std_delta = min_angle = max_angle = 0.0;
    ssr = mse = rms = max_err = 0.0;
}

Angles::Angles(double *A, int nIter, int nAngle) :
    A(A), nIter(nIter), nAngle(nAngle)
{
    if (nAngle == (1 << nIter)) {
        Leaf = 1;
        cout << "A LeafAngles Object is created " ;
    } else {
        Leaf = 0;
        cout << "An AllAngles Object is created " ;
    }

    cout << "(nIter = " << nIter << ", ";
    cout << "nAngle = " << nAngle << ")" <<endl;

    avg_delta = std_delta = min_angle = max_angle = 0.0;
    ssr = mse = rms = max_err = 0.0;

    threshold = 0.0;
}

void Angles::setNIter(int nIter)
{
    nIter = nIter;
}

void Angles::setNAngle(int nAngle)
{
    nAngle = nAngle;
}

void Angles::setThreshold(double th)
{
    threshold = th;
}

```

```
int Angles::getNIter()
{
    return nIter;
}

int Angles::getNAngle()
{
    return nAngle;
}

double Angles::getThreshold()
{
    return threshold;
}

/*****

for (i=0; i<20; i+=4) {
    for (j=0; j<4; ++j) {
        r = atan( 1. / (1 << (i+j)) ) / atan( 1. / (1 << i) ) * 100;
        cout << "index = " << i+j << " --> r = " << r << endl;
    }
}

return 0;
}

*****/

:::::::::::::
Angles_tb.cpp
:::::::::::::
# include <cstdlib>
# include <cmath>
# include <iostream>
# include <iomanip>
# include <fstream>

using namespace std;

# include "cordic.hpp"
# include "Angles.hpp"

string GnuTerm;

//-----
// Purpose:
//
// Explore Angles Space using Class Angles
//
// Discussion:
//
//
// Licensing:
//
```

```
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----
```

```
int main (int argc, char * argv[])
{
    // -----
    // nIter   : Number of Iteration = Height of binary angle tree
    // nAngle  : Number of Angles   = Number of Leaf Nodes
    // -----
    int   nIter = 20;
    int   nAngle = 1 << nIter;
    double th = 0.0;

    // GnuTerm = "wxt";
    GnuTerm = "emf";

    if (argc > 1 ) {
        nIter = atoi(argv[1]);
        nAngle = 1 << nIter;
    }

    if (argc > 2) {
        GnuTerm = argv[2];
    }

    if (argc > 3) {
        th = atof(argv[3]);
    }

    cout << "-----\n";
    cout << "Angles_tb [nIter] [GnuTerm] [th]" << endl;
    cout << "-----\n";
    cout << "        nIter   = " << nIter << " ";
    cout << "        nAngle  = " << nAngle << endl;
    cout << "        GnuTerm = " << GnuTerm << endl;
    cout << "        th      = " << th << endl;
    cout << "-----\n";

    // -----
    // A   : contains the angles of leaf nodes in binary angle tree
    // All : contains the angles of all nodes in binary angle tree
    // -----
    double *A, *All;
    int   level, leaves;
    int   i, j, k;

    A = (double *) malloc ((1<<nIter) * sizeof (double));
    All = (double *) malloc (2* (1<<nIter) * sizeof (double));
```

```

for (j=0; j<nAngle; ++j) {
  A[j] = compute_angle(j, nIter);
  // cout << "A[" << j << "]=" << setw(12) << setprecision(8) << A[j] << endl;
}

for (i=0, k=0; i<=nIter; ++i) {
  level = i;
  leaves = 1 << level;

  // cout << "level = " << level << "leaves = " << leaves << endl;

  for (j=0; j<leaves; ++j) {
    All[j+k] = compute_angle(j, level);
    // cout << "All[" << j+k << "] = " << All[j+k] << endl;
  }

  k += leaves;
}

// -----
// LeafAngles : Angles Class for leaf nodes only
// AllAngles  : Angles Class for all nodes (internal nodes included)
// -----
Angles LeafAngles(A, nIter, nAngle);
Angles AllAngles(All, nIter, 2*nAngle-1);

#ifdef FULLSIM
// -----
// Plot Binary Angle Tree
// -----
draw_angle_tree (nIter, nAngle);

// -----
// Plot angle vectors on a unit circle
// -----
LeafAngles.plot_circle_angle();
AllAngles.plot_circle_angle();

// -----
// Plot angle vectors on a linear scale
// -----
LeafAngles.plot_line_angle();
AllAngles.plot_line_angle();
#endif

LeafAngles.setThreshold(th);
AllAngles.setThreshold(th);

// -----
// Find Angles Statistics --> member data
// -----
LeafAngles.calc_statistics();
AllAngles.calc_statistics();

// -----
// Plot Quantization Effects
// -----
LeafAngles.plot_quantization();
AllAngles.plot_quantization();

```

```
return 0;

// -----
// Plot Delta Distribution & Angle-Delta
// -----
LeafAngles.plot_statistics();
AllAngles.plot_statistics();

// -----
// plot residual errors
// Residuals-Angle Plot & Residuals-Index Plot
// -----
LeafAngles.plot_residual_errors();
AllAngles.plot_residual_errors();

// -----
// Calculate Uniform Scale Statistics --> member data
// -----
LeafAngles.calc_uscale_statistics(1.0, 1.0);
AllAngles.calc_uscale_statistics(1.0, 1.0);

// -----
// Plot Uniform Scale Statistics
// -----
LeafAngles.plot_uscale_statistics();
AllAngles.plot_uscale_statistics();

// -----
// Plot residue errors at the leaf node angles
// -----
LeafAngles.plot_uscale_residual_errors(1, 2);
AllAngles.plot_uscale_residual_errors(1, 2);

return 0;
}
```

```
:::::::::::::
Angles.1.plot_circle_angle.cpp
:::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"

using namespace std;
```

```

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//-----

//-----
// Plot angle vectors on the unit circle
//-----
void Angles::plot_circle_angle ()
{
    int i;
    ofstream myout;

    cout << "* plot_circle_angle ... " ;
    if (Leaf) cout << "(LeafAngles)" << endl;
    else cout << "(AllAngles)" << endl;

    if (nIter > 10) {
        cout << "nIter = " << nIter << " is too large to plot! " << endl;
        return;
    }

    // writing angle data on a unit circle
    myout.open("angle.dat");
    for (i=0; i<nAngle; i++) {
        myout << "0.0 0.0 " << cos(A[i]) << " " << sin(A[i]) << " " << endl;
    }
    myout.close();

    // writing gnuplot commands
    myout.open("command.gp");
    myout << "set terminal " << GnuTerm << endl;
    if (Leaf) {
        myout << "set output 'eg03.leaf.ang_circle.emf'" << endl;
        myout << "set title \"Leaf Angles on a unit circle \" " << endl;
    } else {
        myout << "set output 'eg03.all.ang_circle.emf'" << endl;
        myout << "set title \"All Angles on a unit circle \" " << endl;
    }
    myout << "set xlabel \"x\" " << endl;
    myout << "set ylabel \"y\" " << endl;
    myout << "set size square" << endl;
    myout << "set xrange [-1:+1]" << endl;
    myout << "set yrange [-1:+1]" << endl;
}

```



```

myout << "set object 1 circle at 0, 0 radius 1" << endl;
myout << "plot 'angle.dat' using 1:2:3:4 ";
myout << "with vectors head filled lt 3" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

```

```

system("gnuplot command.gp");

```

```

return;

```

```

}

```

```

:::::::::::::
Angles.2.plot_line_angle.cpp
:::::::::::::

```

```

# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

```

```

# include "Angles.hpp"

```

```

using namespace std;

```

```

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

```

```

//-----
// Plot angle vectors on a linear scale
//-----

```

```

void Angles::plot_line_angle ()
{

```

```

    ofstream myout;

```

```

    cout << "* plot_line_angle ... ";
    if (Leaf) cout << "(LeafAngles)" << endl;
    else cout << "(AllAngles)" << endl;

```

```

    if (nIter > 10) {

```

```

    cout << "nIter = " << nIter << " is too large to plot! " << endl;
    return;
}

// cout << "nIter = " << nIter << endl;
// cout << "nAngle = " << nAngle << endl;

myout.open("angle.dat");

for (int i=0; i<nAngle; ++i) {
    // cout << "A[" << i << "] = " << A[i] << endl;
    myout << A[i] << " 0.0 0.0 1.0" << endl;
}

myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set title \"Leaf Angles on a linear scale\" " << endl;
    myout << "set output 'eg04.leaf.ang_line.emf'" << endl;
} else {
    myout << "set title \"All Angles on a linear scale\" " << endl;
    myout << "set output 'eg04.all.ang_line.emf'" << endl;
}
myout << "set xlabel \"angles in radian\" " << endl;
myout << "set ylabel \"\" " << endl;
myout << "set yrange [0:+2]" << endl;
myout << "plot 'angle.dat' using 1:2:3:4 ";
myout << "with vectors head filled lt 3" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

return;
}

:::::::::::::
Angles.3.calc_statistics.cpp
:::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"

using namespace std;

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:

```

```

//
//   This code is distributed under the GNU LGPL license.
//
// Modified:
//
//   2013.01.17
//
// Author:
//
//   Young Won Lim
//
// Parameters:
//
//-----
//-----
// Find Angles Statistics --> member data
//-----
void Angles::calc_statistics ()
{
    vector <double> B, D;
    vector <double> ::iterator first, last;
    double mean, std;
    ofstream myout;

    cout << "* calc_statistics... ";
    if (Leaf) cout << "(LeafAngles)" << " nAngle = " << nAngle << endl;
    else cout << "(AllAngles)" << " nAngle = " << nAngle << endl;

    for (int i=0; i < nAngle; ++i) {
        // cout << "A[" << i << "]= " << setw(12) << setprecision(8) << A[i] << endl;
        // cout << "B[" << i << "]= " << setw(12) << setprecision(8) << B[i] << endl;
    }

    // B : sorted angles array
    for (int i=0; i < nAngle; ++i)
        B.push_back(A[i]);

    sort(B.begin(), B.end());

    // D : difference angle array
    for (int i=0; i < nAngle-1; ++i)
        D.push_back(B[i+1]- B[i]);

    sort(D.begin(), D.end());

    mean = 0.0;
    for (int i=0; i < D.size(); ++i)
        mean += D[i];
    mean /= D.size();

    std = 0.0;
    for (int i=0; i < D.size(); ++i)
        std += ((D[i]-mean) * (D[i]-mean));
    std /= D.size();
    std = sqrt(std);

    min_angle = B[0];
    max_angle = B[B.size()-1];
    min_delta = D[0];

```

```

max_delta = D[D.size()-1];
avg_delta = mean;
std_delta = std;

double udelta = (B[B.size()-1] - B[0]) / nAngle; // computed uniform delta

cout << "  min angle      = " << min_angle << endl;
cout << "  max angle      = " << max_angle << endl;
cout << "  min delta       = " << min_delta << endl;
cout << "  max delta       = " << max_delta << endl;
cout << "  avg delta       = " << avg_delta << endl;
cout << "  std delta       = " << std_delta << endl;
cout << "  uniform delta   = " << udelta ;
cout << "  = (max-min) / nAngle " << endl;

return;
}

```

```

:::::::::::::
Angles.4.plot_statistics.cpp
:::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"

using namespace std;

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

//-----
// Plot Delta Distribution and Angle-Delta
//-----
void Angles::plot_statistics ()
{

```

```

vector <double> B, D;
vector <double> ::iterator first, last;
double mean, std;
ofstream myout;

cout << "* calc_statistics... ";
if (Leaf) cout << "(LeafAngles)" << " nAngle = " << nAngle << endl;
else cout << "(AllAngles)" << " nAngle = " << nAngle << endl;

for (int i=0; i < nAngle; ++i) {
    // cout << "A[" << i << "]= " << setw(12) << setprecision(8) << A[i] << endl;
    // cout << "B[" << i << "]= " << setw(12) << setprecision(8) << B[i] << endl;
}

// B : sorted angles array
for (int i=0; i < nAngle; ++i)
    B.push_back(A[i]);

sort(B.begin(), B.end());

// D : difference angle array
for (int i=0; i < nAngle-1; ++i)
    D.push_back(B[i+1]- B[i]);

sort(D.begin(), D.end());

double udelta = (B[B.size()-1] - B[0]) / nAngle; // computed unifrom delta

// write histogram data from delta array
myout.open("angle.dat");
double pb ;
for (int i=0, j, k; i<nAngle-2; i++) {
    j = i; k = 1;
    while ((D[j+1] - D[j])/D[j] < 0.01) {
        k++;
        j++;
    }
    pb = (double) k / D.size();
    myout << fixed << right << setw(12) << setprecision(7) << D[i] ;
    myout << " " << pb << endl;
    i = j;
}
myout.close();

cout << " + Delta Distribution Plot \n" ;

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set output 'eg05.leaf.delta_dist.emf'" << endl;
    myout << "set title \"Delta Distribution of Leaf Angles\" " << endl;
} else {
    myout << "set output 'eg05.all.delta_dist.emf'" << endl;
    myout << "set title \"Delta Distribution of All Angles\" " << endl;
}
myout << "set xlabel \"Delta (Adjacent Angle Difference)\" " << endl;
myout << "set ylabel \"probability\" " << endl;
myout << "set yrange [0:+1]" << endl;

myout << "set arrow from " << avg_delta << ", 0";

```

```

myout << " to " << avg_delta << ", 0.7" << endl;
myout << "set label \"avg_delta \" at " << avg_delta;
myout << ", 0.7 right" << endl;

myout << "set arrow from " << udelta << ", 0";
myout << " to " << udelta << ", 0.5" << endl;
myout << "set label \"uniform delta \" at " << udelta;
myout << ", 0.5 right" << endl;

myout << "plot 'angle.dat' with linespoints" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

cout << " + Angle-Delta Plot \n" ;

// write angle-delta data
myout.open("angle.dat");
for (int i=0; i<B.size()-1; i++) {
    myout << B[i] << " " << B[i+1] - B[i] << endl;
}
myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set output 'eg06.leaf.angle_delta.emf'" << endl;
    myout << "set title \"Angle-Delta Plot of Leaf Angles\" " << endl;
} else {
    myout << "set output 'eg06.all.angle_delta.emf'" << endl;
    myout << "set title \"Angle-Delta Plot of All Angles\" " << endl;
}
myout << "set xlabel \"Angles in radian\" " << endl;
myout << "set ylabel \"Delta (Adj Angle Diff) \" " << endl;

myout << "set arrow from " << "-1.0, " << avg_delta;
myout << " to " << "+1.0, " << avg_delta << endl;
myout << "set label \"avg_delta \" at " << "+0.0, ";
myout << avg_delta << " left" << endl;

myout << "set arrow from " << "-1.0, " << udelta;
myout << " to " << "+1.0, " << udelta << endl;
myout << "set label \"uniform delta \" at " << "+1.0, ";
myout << udelta << " left" << endl;

myout << "set arrow from " << "-0.7853, " << min_delta;
myout << "0 to -0.7853, " << max_delta << endl;
myout << "set label \"-pi/4 \" at " << "-0.7853, " ;
myout << min_delta << " right " << endl;

myout << "set arrow from " << "+0.7853, " << min_delta;
myout << "0 to +0.7853, " << max_delta << endl;
myout << "set label \"+pi/4 \" at " << "+0.7853, " ;
myout << min_delta << " left " << endl;

myout << "plot 'angle.dat' with linespoints" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

```

```
    return;
}

::::::::::::
Angles.5.plot_residual_errors.cpp
::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"
# include "cordic.hpp"

using namespace std;

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

//-----
// plot residual errors
// Residuals-Angle Plot and Residuals-Index Plot
//-----
void Angles::plot_residual_errors ()
{
    int i;
    double x, y, z;
    ofstream myout;

    cout << "* plot_residual_errors ... ";
    if (Leaf) cout << "(LeafAngles)" << endl;
    else cout << "(AllAngles)" << endl;

    if (nIter > 10) {
        cout << "nIter = " << nIter << " is too large to plot! " << endl;
        return;
    }
}
```

```

}

// B : sorted angles array
vector <double> B;
vector <double> ::iterator first, last;

for (int i=0; i < nAngle; ++i)
    B.push_back(A[i]);

sort(B.begin(), B.end());

// I=0 Use A[i] for Index-Residuals Plot
// I=1 Use b[i] for Angle-Residuals Plot
//.....
for (int I=0; I<2; I++) {
//.....

// writing residue errors
myout.open("angle.dat");

int nBreak =0;

// not member but local variables
double se, ssr, mse, rms, max_err;
se = ssr = mse = rms = max_err = 0.0;

if (I==0) cout << " + Index-Residuals Plot" << endl;
else      cout << " + Angle-Residuals Plot" << endl;

for (i=0; i<nAngle; i++) {

    x = 1 / K;
    y = 0.0;
    if (I == 0) z = A[i];
    else      z = B[i];

    cordic(&x, &y, &z, nIter, &nBreak, i, threshold);

    se = z * z;
    ssr += se;
    if (se > max_err) max_err = se;

    // cout << "A[" << i << "]=" ;
    // cout << fixed << right << setw(10) << setprecision(7) << A[i];
    // cout << " z=" ;
    // cout << fixed << right << setw(10) << setprecision(7) << z << endl;

    myout << fixed << right << setw(10) << i;
    myout << fixed << right << setw(12) << setprecision(7);
    if (I==0) myout << A[i];
    else      myout << B[i];
    myout << fixed << right << setw(12) << setprecision(7) << z << endl;

}

mse = ssr / nAngle;
rms = sqrt(mse);

max_err = sqrt(max_err);

cout << " No of points = " << nAngle ;
cout << " (nBreak = " << nBreak << " : " ;
cout << 100. * nBreak / nAngle << " % )" << endl;

```



```

cout << "  SSR: Sum of Squared Residuals    = " ;
cout << fixed << right << setw(12) << setprecision(7) << ssr << endl;
cout << "  MSR: Mean Squared Residuals      = " ;
cout << fixed << right << setw(12) << setprecision(7) << mse << endl;
cout << "  RMS: Root Mean Squared Residuals = " ;
cout << fixed << right << setw(12) << setprecision(7) << rms << endl;
cout << "  Max Residual Error                  = " ;
cout << fixed << right << setw(12) << setprecision(7) << max_err << endl;

```

```
myout.close();
```

```
// writing gnuplot commands
```

```
myout.open("command.gp");
```

```

if (I==0) {
    myout << "set terminal " << GnuTerm << endl;
    if (Leaf) {
        myout << "set output 'eg07.leaf.index_res.emf'" << endl;
        myout << "set title \"Index-Residual Plot (Leaf) \" " << endl;
    } else {
        myout << "set output 'eg07.all.index_res.emf'" << endl;
        myout << "set title \"Index-Residual Plot (All) \" " << endl;
    }
    myout << "set xlabel \"Index\" " << endl;
    myout << "set ylabel \"Residuals\" " << endl;
    myout << "plot 'angle.dat' using 1:3 with linespoints " << endl;
} else {
    myout << "set terminal " << GnuTerm << endl;
    if (Leaf) {
        myout << "set output 'eg08.leaf.angle_res.emf'" << endl;
        myout << "set title \"Angle-Residual Plot (Leaf) \" " << endl;
    } else {
        myout << "set output 'eg08.all.angle_res.emf'" << endl;
        myout << "set title \"Angle-Residual Plot of (All)\" " << endl;
    }
    myout << "set xlabel \"Angles\" " << endl;
    myout << "set ylabel \"Residuals\" " << endl;
    myout << "plot 'angle.dat' using 2:3 with linespoints " << endl;
}
myout << "pause mouse keypress" << endl;

```

```
myout.close();
```

```
system("gnuplot command.gp");
```

```

//.....
}
//.....

```

```
return;
```

```
}
```

```

:~::~:
Angles.6.calc_uscale_statistics.cpp
:~::~:

```

```

# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>

```

```

# include <algorithm>

# include "Angles.hpp"
# include "cordic.hpp"

using namespace std;

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

//-----
// Calculate statistics on the uniform scale
//-----
// sssr      : sum of the squares of the residuals
// mse       : mean squared error
// rms       : root mean square error
// max_err   : maximum of squared errors
//-----
// sssr      : sum of the squares of the residuals
// ang = min_angle + avg_delta * offFactor ;
// ang += (avg_delta / resFactor);
//-----
void Angles::calc_uscale_statistics (double resFactor, double offFactor)
{
    int n;
    double x, y, z;
    ofstream myout;

    cout << "* calc_uscale_statistics ... ";
    if (Leaf) cout << "(LeafAngles Resolution)" << endl;
    else cout << "(AllAngles Resolution)" << endl;

    // sr      : square error of a data point

    double ang = min_angle + avg_delta * offFactor ;
    double se = 0.0 ;
    int nBreak =0;
    n = 0;

    sssr = mse = rms = max_err = 0.0;

    while (ang < max_angle) {
        x = 1 / K;

```

```

y = 0.0;
z = ang;

cordic(&x, &y, &z, nIter, &nBreak, n, threshold);

se = (z * z);
ssr += se;
if (se > max_err) max_err = se;

// cout << fixed << right << setw(10) << setprecision(7) << A[i];
// cout << fixed << right << setw(10) << setprecision(7) << z << endl;

ang += (avg_delta / resFactor);
n++;

}

mse = ssr / n;
rms = sqrt(mse);

max_err = sqrt(max_err);

cout << "  Angles = (" ;
cout << min_angle << " : " << avg_delta << " : " << max_angle << ")" ;
cout << endl << "  --> total " << n << " points" ;
cout << " (nBreak = " << nBreak << " : " ;
cout << 100. * nBreak / n << " % )" << endl;

cout << "  SSR: Sum of Squared Residuals    = " ;
cout << fixed << right << setw(12) << setprecision(7) << ssr << endl;
cout << "  MSR: Mean Squared Residuals      = " ;
cout << fixed << right << setw(12) << setprecision(7) << mse << endl;
cout << "  RMS: Root Mean Squared Residuals = " ;
cout << fixed << right << setw(12) << setprecision(7) << rms << endl;
cout << "  Max Residual Error                  = " ;
cout << fixed << right << setw(12) << setprecision(7) << max_err << endl;

return;

}

:::::::::::::
Angles.7.plot_uscale_statistics.cpp
:::::::::::::
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"

using namespace std;

//-----
//  Purpose:
//
//    Class Angles Implementation Files
//
//  Discussion:
//

```

```

//
// Licensing:
//
//   This code is distributed under the GNU LGPL license.
//
// Modified:
//
//   2013.01.17
//
// Author:
//
//   Young Won Lim
//
// Parameters:
//
//-----
//-----
//   Plot uniform scale statistics
//-----
//   ang = min_angle + avg_delta * offFactor ;
//   ang += (avg_delta / resFactor);
//-----
void Angles::plot_uscale_statistics ( )
{
    int    i, j;
    double resFactor, offFactor;
    ofstream myout;

    cout << "* plot_uscale_statistics ... ";
    if (Leaf) cout << "(LeafAngles Resolution)" << endl;
    else cout << "(AllAngles Resolution)" << endl;

    if (nIter > 10) {
        cout << "nIter = " << nIter << " is too large to plot! " << endl;
        return;
    }

    // ssr : sum of the squares of the residuals
    // mse : mean squared error
    // rms : root mean square error
    // sr  : square error of a data point
    // max_err : maximum of squared errors

    int M=4; // no of resFactor's
    int N=4; // no of offFactor's
    double SSR[M][N];

    for (i=0; i<M; i++) {
        resFactor = i + 1.0;

        for (j=0; j<N; j++) {
            offFactor = (j+1) / N;

            cout << " ===== resFactor= " << i << ",   offFactor= " << j ;
            cout << " =====" << endl;

            calc_uscale_statistics(resFactor, offFactor);

            SSR[i][j] = ssr;
        }
    }
}

```

```

// writing residue errors
myout.open("angle.dat");

for (i=0; i<M; i++) {
    cout << i+1 << " ";
    myout << i+1 << " ";
    for (j=0; j<N; j++) {
        cout << SSR[i][j] << " ";
        myout << SSR[i][j] << " ";
    }
    cout << endl;
    myout << endl;
}

myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
myout << "set autoscale y" << endl;
if (Leaf) {
    myout << "set output 'eg09.leaf.resfac_ssr.emf'" << endl;
    myout << "set title \"resFactor-SSR Plot (Leaf) \" " << endl;
} else {
    myout << "set output 'eg09.all.resfac_ssr.emf'" << endl;
    myout << "set title \"resFactor-SSR Plot (All) \" " << endl;
}
myout << "set xlabel \"resFactor\" " << endl;
myout << "set ylabel \"SSR (Sum of Squared Residuals)\" " << endl;
myout << "plot " ;
for (j=0; j<N; j++) {
    myout << " 'angle.dat' using 1:" << j+2 ;
    myout << " title 'offFactor=' << (j+1) << "/" << N << " " ;
    myout << " with linespoints" ;
    if (j<N-1) myout << ", "; else myout << endl;
}

myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

```

```

// writing residue errors
myout.open("angle.dat");

for (j=0; j<N; j++) {
    cout << j+1 << " ";
    myout << j+1 << " ";
    for (i=0; i<M; i++) {
        cout << SSR[i][j] << " ";
        myout << SSR[i][j] << " ";
    }
    cout << endl;
    myout << endl;
}

myout.close();

```

```

// writing gnuplot commands
myout.open("command.gp");

```

```

myout << "set terminal " << GnuTerm << endl;
myout << "set autoscale y" << endl;
myout << "set autoscale y" << endl;
if (Leaf) {
    myout << "set output 'egl0.leaf.offfac_ssr.emf'" << endl;
    myout << "set title \"offFactor-SSR Plot (Leaf) \" " << endl;
} else {
    myout << "set output 'egl0.all.offfac_ssr.emf'" << endl;
    myout << "set title \"offFactor-SSR Plot (All) \" " << endl;
}
myout << "set xlabel \"offFactor\" " << endl;
myout << "set ylabel \"SSR (Sum of Squared Residuals)\" " << endl;
myout << "plot " ;
for (i=0; i<M; i++) {
    myout << " 'angle.dat' using 1:" << i+2 ;
    myout << " title 'resFactor=" << (i+1) << " " ;
    myout << " with linespoints" ;
    if (i<M-1) myout << ", "; else myout << endl;
}

myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

return;
}

```

```

:::::::::::::
Angles.8.plot_uscale_residual_errors.cpp
:::::::::::::

```

```

# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"
# include "cordic.hpp"

```

```
using namespace std;
```

```

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17

```

```

//
// Author:
//
//   Young Won Lim
//
// Parameters:
//
//-----
//-----
//   Plot residual errors on the uniform scale
//-----
//   ang = min_angle + avg_delta * offFactor ;
//   ang += (avg_delta / resFactor);
//-----
void Angles::plot_uscale_residual_errors
(double resFactor, double offFactor )
{
    int n;
    double x, y, z;
    ofstream myout;

    cout << " * plot_uscale_residual_errors ... ";
    if (Leaf) cout << "(LeafAngles Resolution)" << endl;
    else cout << "(AllAngles Resolution)" << endl;

    if (nIter > 10) {
        cout << "nIter = " << nIter << " is too large to plot! " << endl;
        return;
    }

    double ang = min_angle + avg_delta * offFactor ;
    double se = 0.0 ;
    int nBreak =0;
    n = 0;

    // writing residue errors
    myout.open("angle.dat");

    while (ang < max_angle) {
        x = 1 / K;
        y = 0.0;
        z = ang;

        cordic(&x, &y, &z, nIter, &nBreak, n, threshold);

        se = (z * z);

        // cout << fixed << right << setw(10) << setprecision(7) << A[i];
        // cout << fixed << right << setw(10) << setprecision(7) << z << endl;

        myout << fixed << right << setw(10) << n;
        myout << fixed << right << setw(22) << setprecision(7) << ang;
        myout << fixed << right << setw(22) << setprecision(7) << z;
        myout << fixed << right << setw(22) << setprecision(7) << se << endl;

        ang += (avg_delta / resFactor);
        n++;
    }

    cout << " Angles = (" ;
    cout << min_angle << " : " << avg_delta << " : " << max_angle << ")" ;

```

```

cout << endl << " --> total " << n << " points" ;
cout << " (nBreak = " << nBreak << " : " ;
cout << 100. * nBreak / n << " % )" << endl;

myout.close();

// writing gnuplot commands
myout.open("command.gp");
myout << "set autoscale y" << endl;
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set output 'eg11.leaf.idx_res_us.emf'" << endl;
    myout << "set title \"Index-Residual Plot (uScale-Leaf)\"" << endl;
} else {
    myout << "set output 'eg11.all.idx_res_us.emf'" << endl;
    myout << "set title \"Index-Residual Plot (uScale-All)\"" << endl;
}
myout << "set xlabel \"Index\" " << endl;
myout << "set ylabel \"Residuals\" " << endl;
myout << "plot 'angle.dat' using 1:3 with linespoints " << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

// writing gnuplot commands
myout.open("command.gp");
myout << "set autoscale y" << endl;
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set output 'eg12.leaf.ang_res_us.emf'" << endl;
    myout << "set title \"Angle-Residual Plot (uScale-Leaf)\"" << endl;
} else {
    myout << "set output 'eg12.all.ang_res_us.emf'" << endl;
    myout << "set title \"Angle-Residual Plot (uScale-All)\"" << endl;
}
myout << "set xlabel \"Angle\" " << endl;
myout << "set ylabel \"Residuals\" " << endl;
myout << "plot 'angle.dat' using 2:3 with linespoints " << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

return;
}

void Angles::plot_uscale_residual_errors ()
{
    plot_uscale_residual_errors (1.0, 1.0);
}

```

```

:::::::::::::
Angles.9.plot_quantization.cpp
:::::::::::::

```



```
# include <iostream>
# include <iomanip>
# include <cstdlib>
# include <cmath>
# include <fstream>
# include <vector>
# include <algorithm>

# include "Angles.hpp"
# include "cordic.hpp"

using namespace std;

//-----
// Purpose:
//
// Class Angles Implementation Files
//
// Discussion:
//
//
// Licensing:
//
// This code is distributed under the GNU LGPL license.
//
// Modified:
//
// 2013.01.17
//
// Author:
//
// Young Won Lim
//
// Parameters:
//
//-----

//-----
// Plot Non-uniform Quantization of CORDIC
//-----
void Angles::plot_quantization ()
{

vector <double> B, D;
vector <double> ::iterator first, last;
double mean, std;
ofstream myout;

cout << "* calc_statistics... ";
if (Leaf) cout << "(LeafAngles)" << " nAngle = " << nAngle << endl;
else cout << "(AllAngles)" << " nAngle = " << nAngle << endl;

for (int i=0; i < nAngle; ++i) {
// cout << "A[" << i << "]= " << setw(12) << setprecision(8) << A[i] << endl;
// cout << "B[" << i << "]= " << setw(12) << setprecision(8) << B[i] << endl;
}

// B : sorted angles array
for (int i=0; i < nAngle; ++i)
B.push_back(A[i]);

sort(B.begin(), B.end());
```

```
// D : difference angle array
for (int i=0; i < nAngle-1; ++i)
    D.push_back(B[i+1]- B[i]);

sort(D.begin(), D.end());

double udelta = (B[B.size()-1] - B[0]) / nAngle; // computed unifrom delta

// write histogram data from delta array
myout.open("angle.dat");
double pb ;
for (int i=0; i<nAngle; i++) {
    myout << fixed << right << setw(12) << setprecision(7) << B[0] + udelta*i ;
    myout << fixed << right << setw(12) << setprecision(7) << B[0] + udelta*i ;
    myout << fixed << right << setw(12) << setprecision(7) << B[i] ;
    myout << " " << endl;
}
myout.close();

cout << " + Quantization Effect Plot \n" ;

// writing gnuplot commands
myout.open("command.gp");
myout << "set terminal " << GnuTerm << endl;
if (Leaf) {
    myout << "set output 'eg12.leaf.quantization.emf'" << endl;
    myout << "set title \"Quantization Effect of Leaf Angles\" " << endl;
} else {
    myout << "set output 'eg12.all.quantization.emf'" << endl;
    myout << "set title \"Quantization Effect of All Angles\" " << endl;
}
myout << "set xlabel \"Delta (Adjacent Angle Difference)\" " << endl;
myout << "set ylabel \"Quantized Angles\" " << endl;
myout << "set yrange [" << B[0] << ":" << B[B.size()-1] << "]" << endl;

myout << "plot 'angle.dat' using 1:2 with lines, ";
myout << " 'angle.dat' using 1:3 with lines" << endl;
myout << "pause mouse keypress" << endl;
myout.close();

system("gnuplot command.gp");

return;
}
```