## Anti-aliasing Prefilter (6B)

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## Sampler

Ideal Sampling


$$
\hat{x}(t)=\sum_{n=-\infty}^{+\infty} x(n T) \delta(t-n T)
$$

CTFT

$$
\hat{X}(f)=\int_{-\infty}^{+\infty} \hat{x}(t) e^{-j 2 \pi f t} d t
$$

## Practical Sampling


$\hat{x}(t) \approx \sum_{n=-\infty}^{+\infty} x(n T) p(t-n T)$
CTFT


## Zero Order Hold (ZOH)




$$
x_{\text {ZOH }}(t)=\sum_{n=-\infty}^{+\infty} x[n] \cdot \operatorname{rect}\left(\frac{t-T / 2-n T}{T}\right)
$$

## Time Sequence



$$
\hat{x}(t)
$$



$$
\begin{gathered}
\nabla \\
\cdots \\
x[n]
\end{gathered}
$$

Ideal
Sampling


$$
p(t)=\sum_{n=-\infty}^{+\infty} \delta(t-n T)
$$

$T$ Sampling Period

$$
\begin{aligned}
& p(t) \\
& \underset{T}{\Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta \Delta}
\end{aligned}
$$



$$
\frac{2}{4} f_{s} \quad \frac{3}{4} f_{s}
$$

## References

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