Introduction to Systems of Linear Equations

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2-dim \Longrightarrow Line equation a x + b y = c (a, b not both 0)



n-dim
$$\rightarrow$$
 Hyper-Plane equation
 $a_1 x_1 + a_2 x_2 + \dots + a_n x_n = b$ (a not both 0)
(n=2) $a_1 x_1 + a_2 x_2 = b$ $\rightarrow a x + b y = c$
(n=3) $a_1 x_1 + a_2 x_2 + a_3 x_3 = b$ $\rightarrow a x + b y + c z = d$

Homogeneous Linear Equations

2-dim \rightarrow Line equation a x + b y = 0 (a, b not both 0)



n-dim
$$\longrightarrow$$
 Hyper-Plane equation
 $a_1 x_1 + a_2 x_2 + \dots + a_n x_n = 0$ (a, not both 0)
(n=2) $a_1 x_1 + a_2 x_2 = 0$ $a x + b y = 0$
(n=3) $a_1 x_1 + a_2 x_2 + a_3 x_3 = 0$ $a x + b y + c z = 0$

Linear Systems

System of Linear Equation



Linear Systems of 2 Unknowns

(Eq 1)
$$\rightarrow$$
 a_{11} x_1 + a_{12} x_2 = b_1
(Eq 2) \rightarrow a_{21} x_1 + a_{22} x_2 = b_2



Linear Systems of 2 Unknowns



7

Introduction

Linear Systems of 3 Unknowns



Introduction

$$a_{11}$$
 x_1 + a_{12} x_2 + ... + a_{1n} x_n = b_1

$$\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \end{bmatrix}$$

$$\begin{bmatrix} n \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$\begin{bmatrix} row index \\ nx1 \ Vector \\ nx1 \ Vector \end{bmatrix}$$



$$a_{m1} x_{1} + a_{m2} x_{2} + \cdots + a_{mn} x_{n} = b_{m}$$

$$\begin{bmatrix} a_{m1} & a_{m2} & \cdots & a_{mn} \\ \vdots \\ x_{n} \end{bmatrix} = b_{m}$$

$$\begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n} \end{bmatrix}$$

$$\begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n} \end{bmatrix}$$

$$\begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n} \end{bmatrix}$$

$$\begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n} \end{bmatrix}$$

Storing Magnetic Energy

References

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- [2] Anton, et al., Elementary Linear Algebra, 10th ed, Wiley, 2011
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