Bandpass Sampling (2B)

- - •

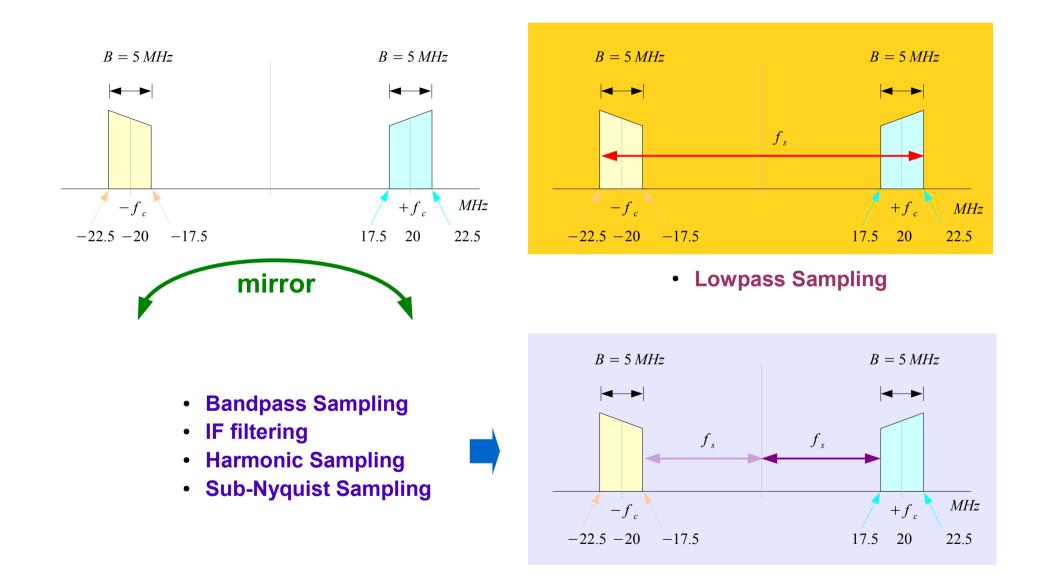
Copyright (c) 2009 - 2012 Young W. Lim.

Permission is granted to copy, distribute and/or modify this document under the terms of the GNU Free Documentation License, Version 1.2 or any later version published by the Free Software Foundation; with no Invariant Sections, no Front-Cover Texts, and no Back-Cover Texts. A copy of the license is included in the section entitled "GNU Free Documentation License".

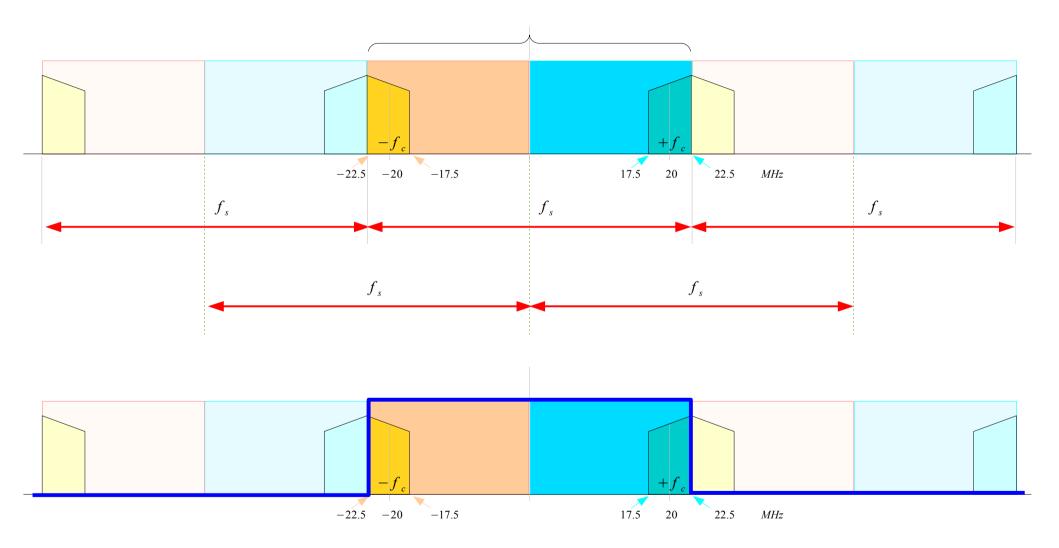
Please send corrections (or suggestions) to youngwlim@hotmail.com.

This document was produced by using OpenOffice and Octave.

Band-limited Signal

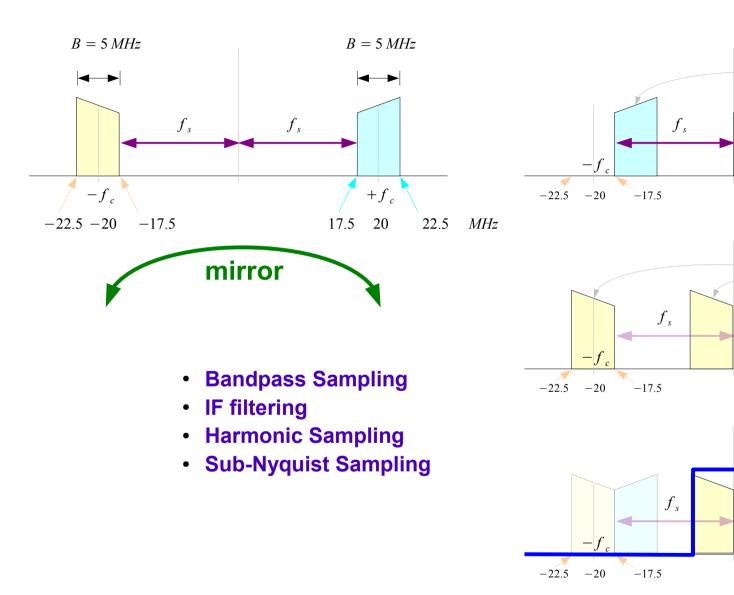


Low-pass Signal Sampling



4

Band-pass Signal Sampling



Young Won Lim 3/8/12

 f_s

 f_s

 f_s

 $+f_c$

20

 $+f_c$

20

+

20

22.5

22.5

22.5

MHz

MHz

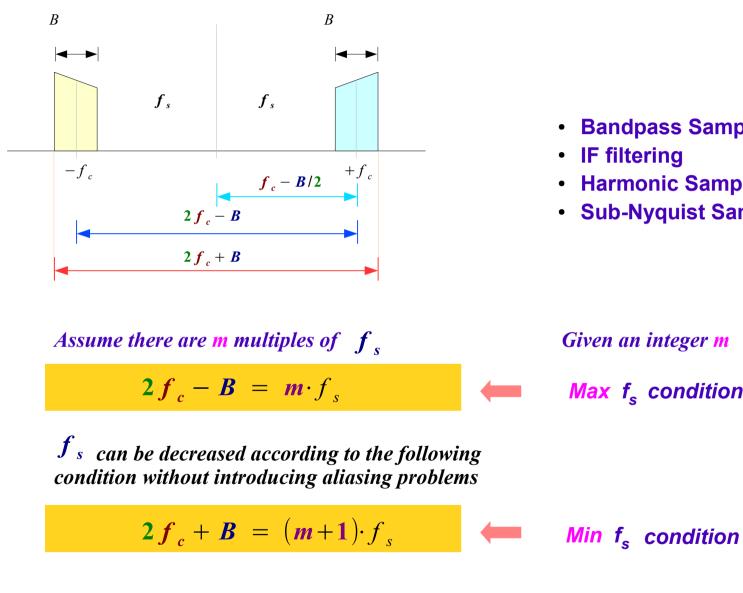
MHz

17.5

17.5

17.5

Range of Sampling Frequency $f_{s}(1)$

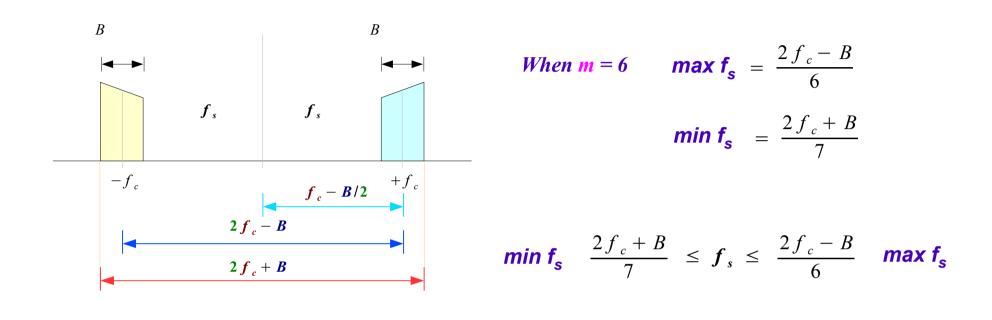


- Bandpass Sampling
- IF filtering
- Harmonic Sampling
- Sub-Nyquist Sampling

Given an integer m Max f_s condition

6

Range of Sampling Frequency f_s (2)



Assume there are *m* multiples of f_s

 $2f_c - B = m \cdot f_s$

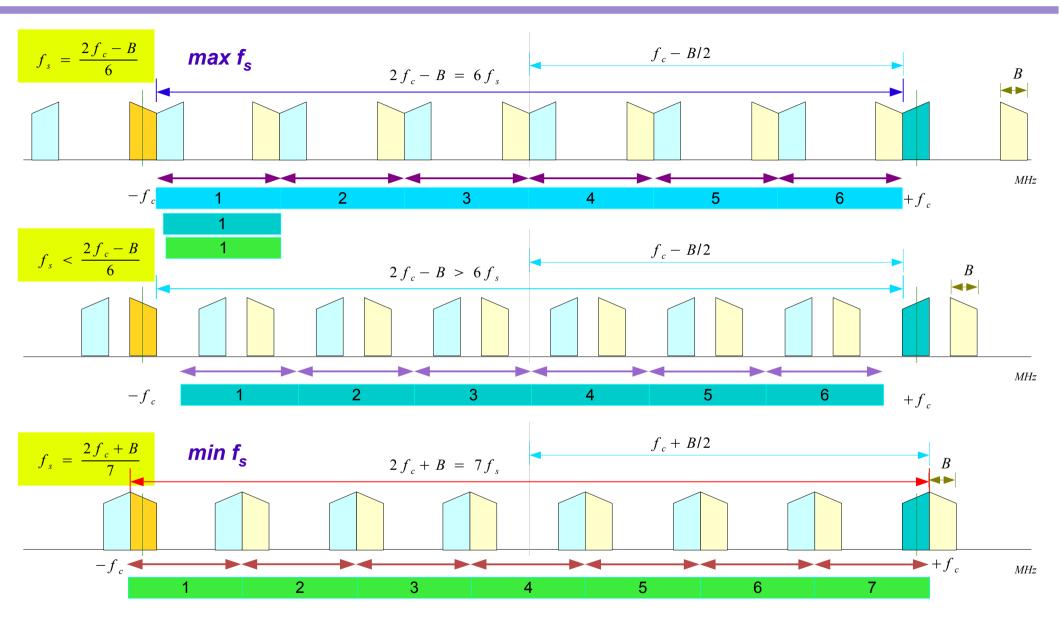
Given an integer m Max f_s condition

 f_s can be decreased according to the following condition without introducing aliasing problems

$$2f_c + B = (m+1) \cdot f_s$$

Min f_s condition

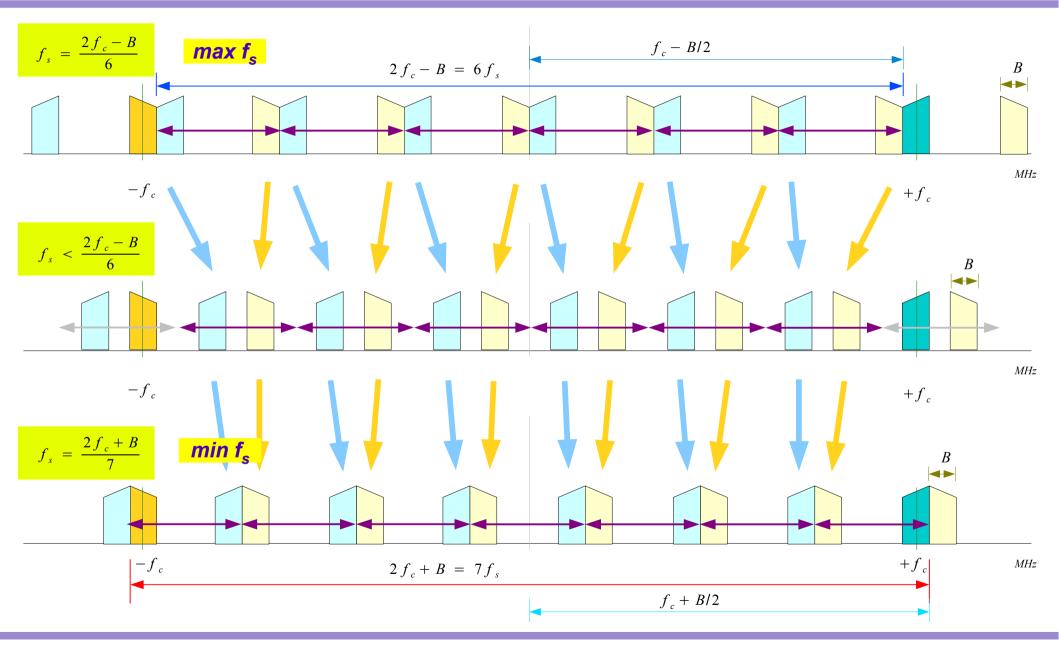
Range of Sampling Frequency f_s (3)



2B Bandpass Sampling

8

Range of Sampling Frequency f_s (4)



2B Bandpass Sampling

Range of Sampling Frequency f_s (5)

$$\frac{2 f_c + B}{m + 1} \le f_s \le \frac{2 f_c - B}{m}$$

$$f_c = 20 MHz$$

$$B = 5 MHz$$

$$2B \le f_s$$

$$m = 1 \implies \frac{2 \cdot 20 + 5}{1 + 1} = 22.5 \le f_s \le \frac{2 \cdot 20 - 5}{1} = 35$$

$$f_s = 22.5 MHz$$

$$(10 \le f_s)$$

$$m = 2 \implies \frac{2 \cdot 20 + 5}{2 + 1} = 15 \le f_s \le \frac{2 \cdot 20 - 5}{2} = 17.5$$

$$f_s = 17.5 MHz$$

$$(10 \le f_s)$$

$$m = 3 \implies \frac{2 \cdot 20 + 5}{3 + 1} = 11.25 \le f_s \le \frac{2 \cdot 20 - 5}{3} = 11.67$$

$$f_s = 11.25 MHz$$

$$(10 \le f_s)$$

$$m = 4 \implies \frac{2 \cdot 20 + 5}{4 + 1} = 9$$

$$\geq \frac{2 \cdot 20 - 5}{4} = 8.75$$

$$M = 5 \implies \frac{2 \cdot 20 + 5}{5 + 1} = 7.5$$

$$\geq \frac{2 \cdot 20 - 5}{5} = 7.0$$

$$M = 5 \implies \frac{2 \cdot 20 + 5}{5 + 1} = 7.5$$

$$\geq \frac{2 \cdot 20 - 5}{5} = 7.0$$

Range of Sampling Frequency f_s (6)

$$\frac{2f_c + B}{m+1} \leq f_s \leq \frac{2f_c - B}{m} \qquad f_c = 20 \text{ MHz}$$

$$B = 5 \text{ MHz}$$

$$\frac{f_c + B/2}{B} = R \qquad \frac{\text{highest signal frequency}}{\text{bandwidth}}$$

$$\frac{2f_c + B}{(m+1)B} = f(m, R) \qquad \frac{\text{minimum sampling rate}}{\text{bandwidth}}$$

$$\frac{2(f_c + B/2)}{(m+1)B} = \frac{2R}{m+1} = f(m, R) \qquad m = 1 \quad f(1, R) = R \qquad m = 5 \quad f(5, R) = \frac{1}{3}R$$

$$m = 2 \quad f(2, R) = \frac{2}{3}R \qquad m = 6 \quad f(6, R) = \frac{2}{7}R$$

$$m = 4 \quad f(4, R) = \frac{1}{2}R \qquad m = 8 \quad f(8, R) = \frac{2}{9}R$$

Range of Sampling Frequency $f_s(7)$

$$\frac{2f_c + B}{m+1} \le f_s \le \frac{2f_c - B}{m}$$

$$f_c = 20 MHz$$

$$B = 5MHz$$

$$2B \le f_s$$

$$\frac{f_c + B/2}{B} = R$$

$$\frac{highest signal frequency}{bandwidth}$$

$$f_H = f_c + B/2$$

$$R = f_H / B$$

$$\frac{2f_c + B}{m+1} \cdot \frac{1}{B} = f(m, R)$$

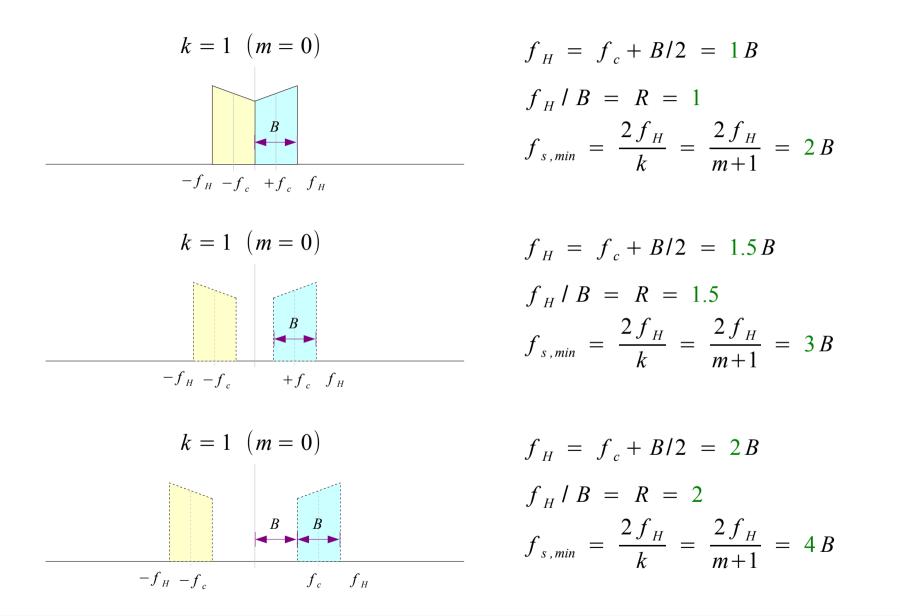
$$\frac{minimum sampling rate}{bandwidth}$$

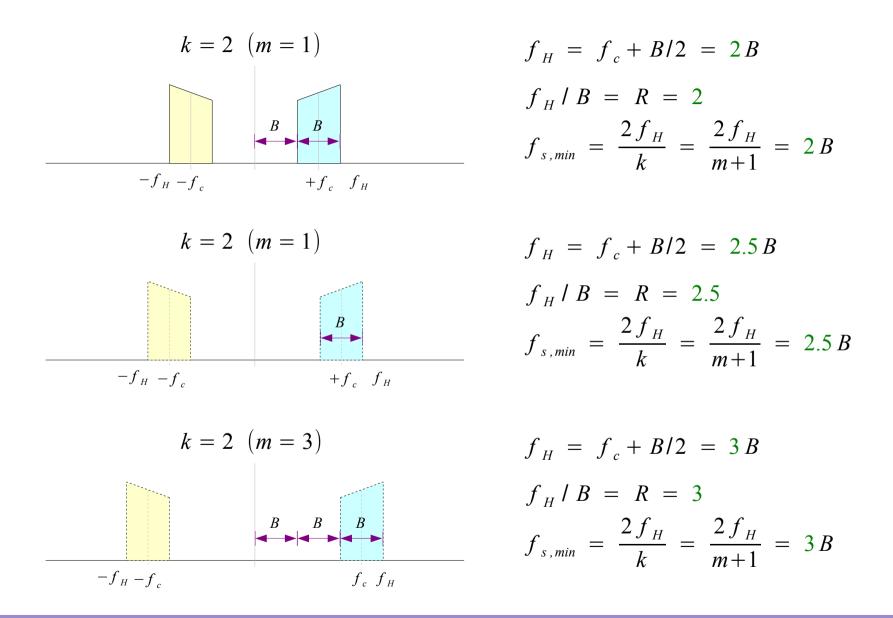
$$f(m, R) = \frac{2f_c + B}{m+1} = \frac{2f_H}{k}$$

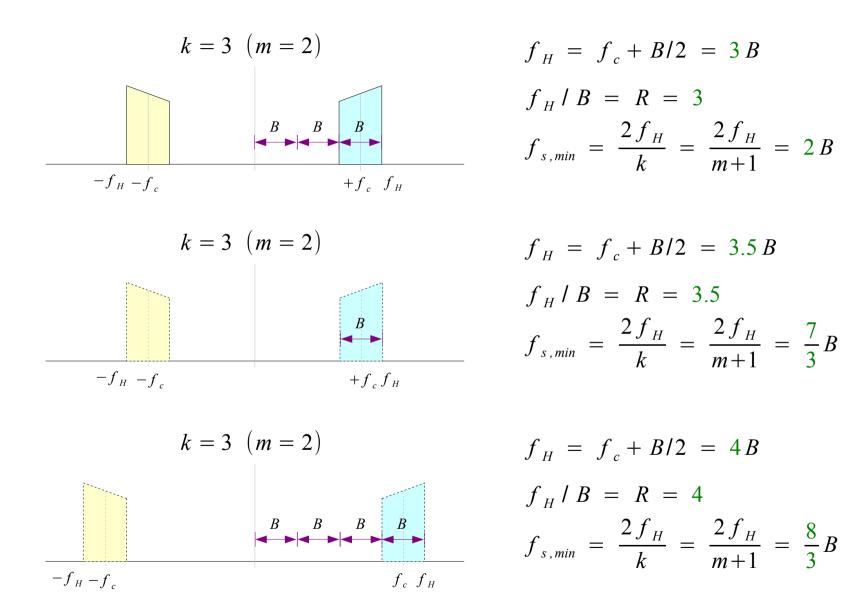
$$f(m, R) = \frac{2f_H}{kB} = \frac{2R}{k}$$

$$m+1 = k$$

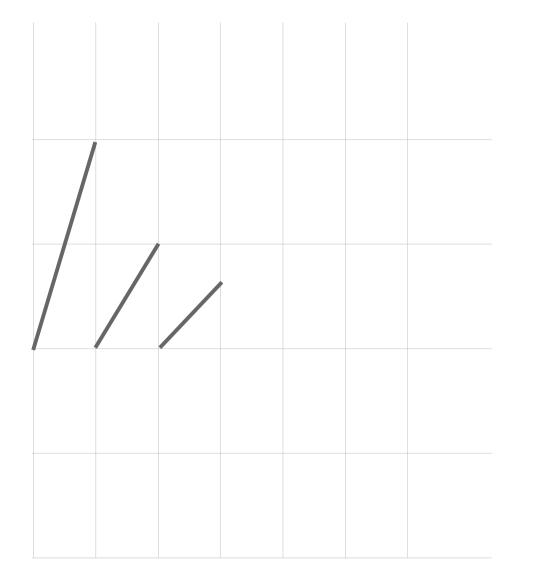
$$\frac{g_{h}}{f_{h}} = \frac{1}{2R}$$







Young Won Lim 3/8/12



References

- [1] http://en.wikipedia.org/
- [2] J.H. McClellan, et al., Signal Processing First, Pearson Prentice Hall, 2003
- [3] A "graphical interpretation" of the DFT and FFT, by Steve Mann
- [4] R. G. Lyons, Understanding Digital Signal Processing, 1997