## Elementary Matrix

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## Gauss-Jordan Elimination

Forward Phase - Gaussian Elimination


Backward Phase
$\left(\begin{array}{ccc|c}+1 & +1 / 2 & -1 / 2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & +1 & -1\end{array}\right) \Rightarrow\left[\begin{array}{ccc|c}+1 & +1 / 2 & 0 & +7 / 2 \\ 0 & +1 & 0 & +3 \\ 0 & 0 & +1 & -1\end{array}\right) \Rightarrow\left(\begin{array}{ccc|c}+1 & 0 & 0 & +2 \\ 0 & +1 & 0 & +3 \\ 0 & 0 & +1 & -1\end{array}\right)$

## Elementary Row Operation

Interchange two rows


Multiply a row by a nonzero constant


Add a multiple of one row to another


## Elementary Matrix

Identity Matrix
$\left(\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right)$

Interchange two rows


Multiply a row by a nonzero constant


Add a multiple of one row to another


## Multiplication by an Elementary Matrix

$$
\begin{aligned}
& {\left[\begin{array}{lll}
0 & 1 & 0 \\
1 & 0 & 0 \\
0 & 0 & 1
\end{array}\right] \quad\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right] \quad\left[\begin{array}{lll}
4 & 5 & 6 \\
1 & 2 & 3 \\
7 & 8 & 9
\end{array}\right]} \\
& {\left[\begin{array}{lll}
3 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right] \quad\left[\begin{array}{lll}
3 & 6 & 9 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right]} \\
& {\left[\begin{array}{lll}
1 & 0 & 0 \\
4 & 1 & 0 \\
0 & 0 & 1
\end{array}\right] \quad\left[\begin{array}{lll}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{array}\right] \quad\left[\begin{array}{ccc}
1 & 2 & 3 \\
8 & 13 & 18 \\
7 & 8 & 9
\end{array}\right]}
\end{aligned}
$$

## Pulse

## References

[1] http://en.wikipedia.org/
[2] Anton \& Busby, "Contemporary Linear Algebra"

