Binary Angle Measurement (5A)

- Adaptive CORDIC
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BAM Background

T.K. Rodrigues, "Adaptive CORDIC: Using Parallel Angle Recording to Accelerate Rotations", IEEE Trans on Computers, 2010

Rotation of 25 degree

Original CORDIC

$$25^{\circ} \approx +45^{\circ}$$

$$-26.565^{\circ}$$

$$+14.036^{\circ}$$

$$-7.125^{\circ}$$

$$-3.576^{\circ}$$

$$+1.79^{\circ}$$

$$+0.895^{\circ}$$

$$+0.448^{\circ}$$

$$+0.2238^{\circ}$$

$$= 25.1268^{\circ}$$

Angle Constants that is used

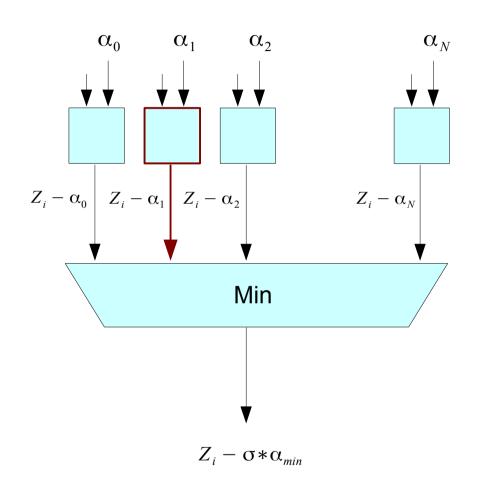
$$Q = \{45^{\circ}, 26.565^{\circ}, 14.036^{\circ}, 7.125^{\circ}, 3.576^{\circ}, 1.79^{\circ}, 0.895^{\circ}, 0.448^{\circ}, 0.2238^{\circ}\}$$

Range of Residual Angles around Angle Constant

45° >35	5.78	(45+26.565)	$[Z_{45}{}^{\circ}]$	=	[35.78, 6	57.5]
26.565° <>20	0.295	2	$[Z_{26.565}{}^{\circ}]$	=	[20.295,	35.78]
14.036 ° <	0.5775		$[Z_{14.036}^{\circ}]$	=	[10.5775,	20.295]
7.125°	5.5305		$[Z_{7.125}^{}$ $^{\circ}]$	=	[5.3505,	10.5775]
3.576° <> 2	2.6825		$[Z_{3.576}^{\circ}]$	=	[2.6825,	5.3505]
1.79°	1.342		$[Z_{1.79}^{\circ}]$	=	[1.342, 2	2.6825]
0.895°	0.6715		$[Z_{0.895^{\circ}}]$	=	[0.6715,	1.342]
0.448°	0.3359		$[Z_{0.448}{}^{\circ}]$	=	[0.3359,	0.6715]
0.2238°).1119		$[Z_{0.2238}$ ° $]$	=	[0.1119,	0.3359]

Angle Recording Method

```
\alpha \leftarrow \alpha_N
Z \leftarrow \theta
while (|Z| > \alpha_{min}/2) {
      \sigma = (Z \ge 0) ? +1 : -1;
      foreach \alpha_i (\alpha_0, \alpha_1, \cdots, \alpha_N) {
           if (||Z| - \alpha_i| < ||Z| - \alpha_{max}|) {
                  \alpha_{min} = \alpha_i
           Store \alpha_{max} on adaptive—angle—list
          Z = Z - \sigma * \alpha_{max}
```

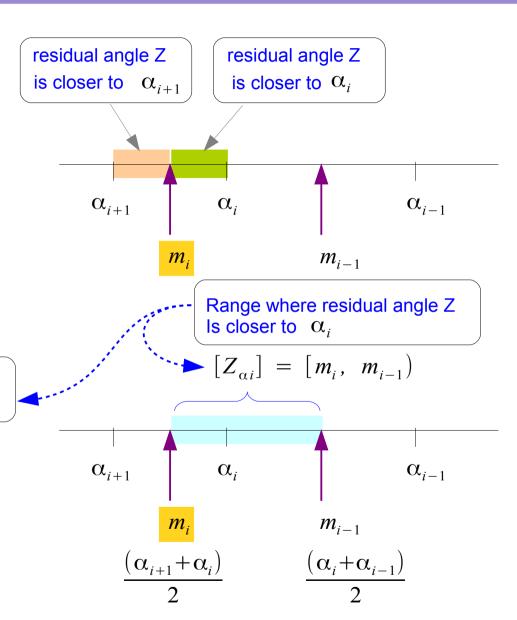


Range

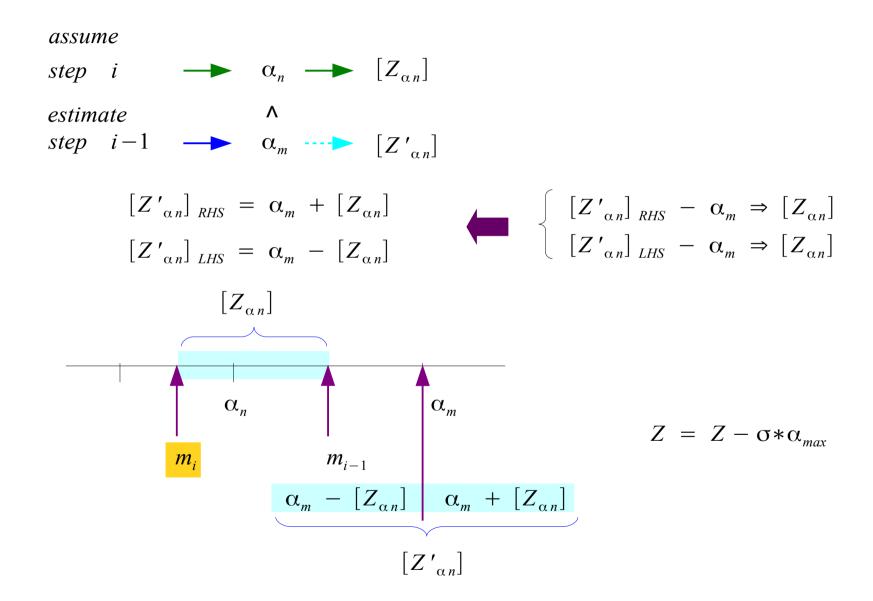
$$\boxed{m_i = \frac{(\alpha_{i+1} + \alpha_i)}{2}}$$

$$[Z_{\alpha i}] = [m_i, m_{i-1})$$

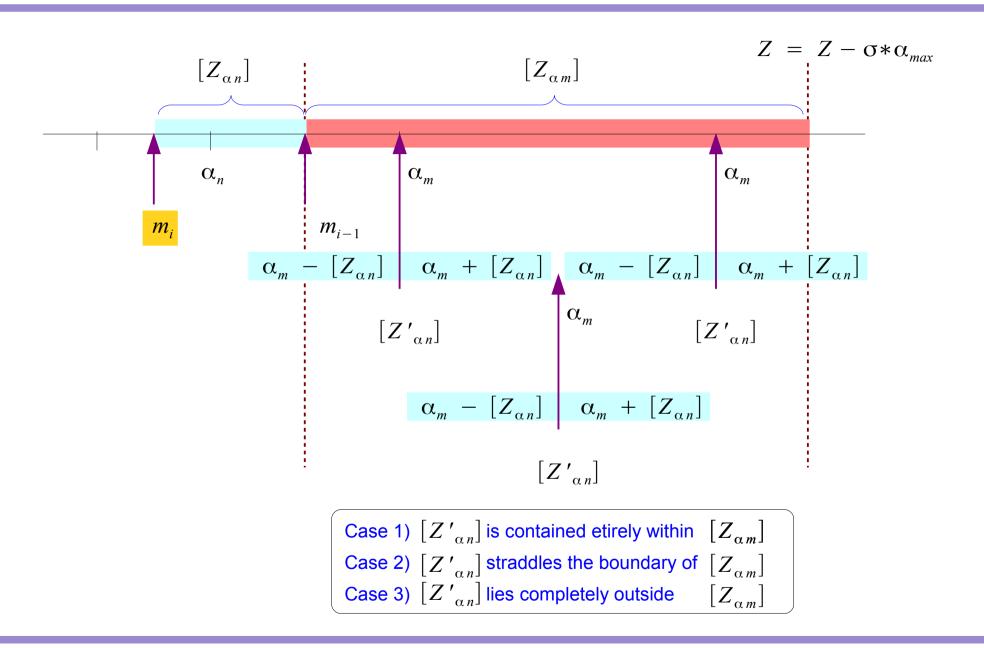
Angle Recording selects the angle constant $\,\alpha_i\,$ for the angles in the range $\,[Z_{\alpha\,n}]\,$



Estimated Range



Conditions of Estimated Range



CORDIC Rotation

References

- [1] http://en.wikipedia.org/
- [2] CORDIC FAQ, www.dspguru.com
- [3] R. Andraka, A survey of CORDIC algorithms for FPGA based computers
- [4] J. S. Walther, A Unified Algorithm for Elementary Functions
- [5] J. P. Deschamps, G. A. Bioul, G.D. Sutter, Synthesis of Arithmetic Circuits
- [6] T.K. Rodrigues, "Adaptive CORDIC: Using Parallel Angle Recording to Accelerate Rotations", IEEE Trans on Computers, 2010