# Upsampling (5B)

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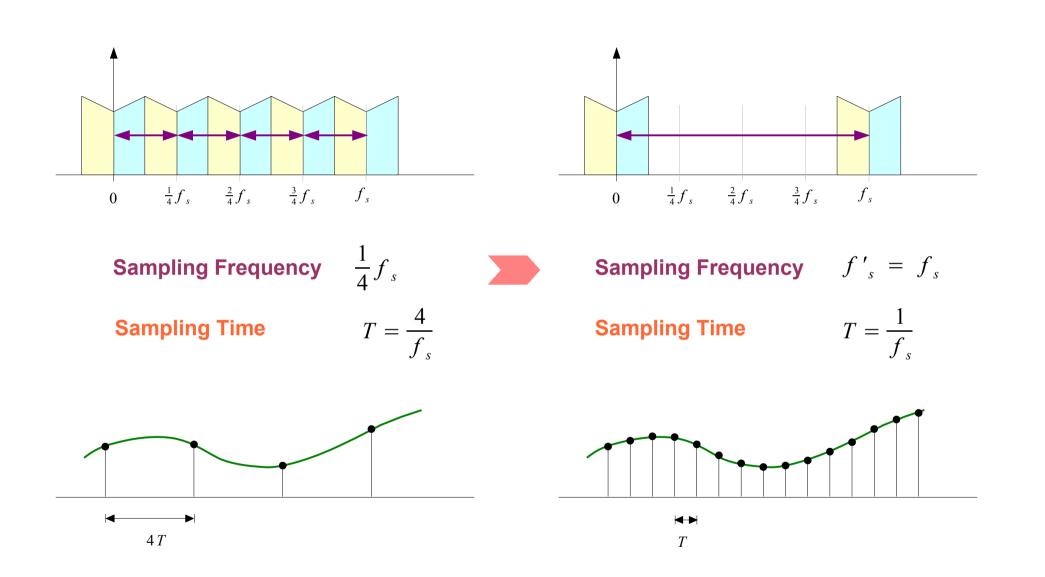
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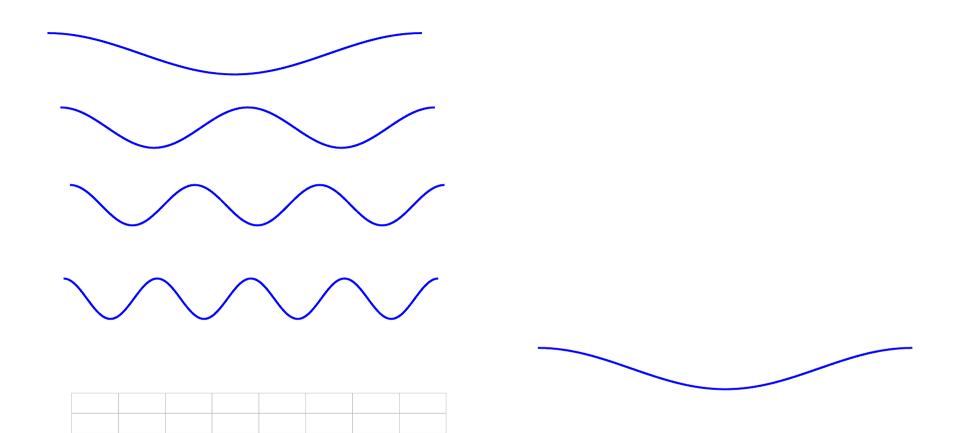
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#### **Band-limited Signal**



#### Measuring Rotation Rate

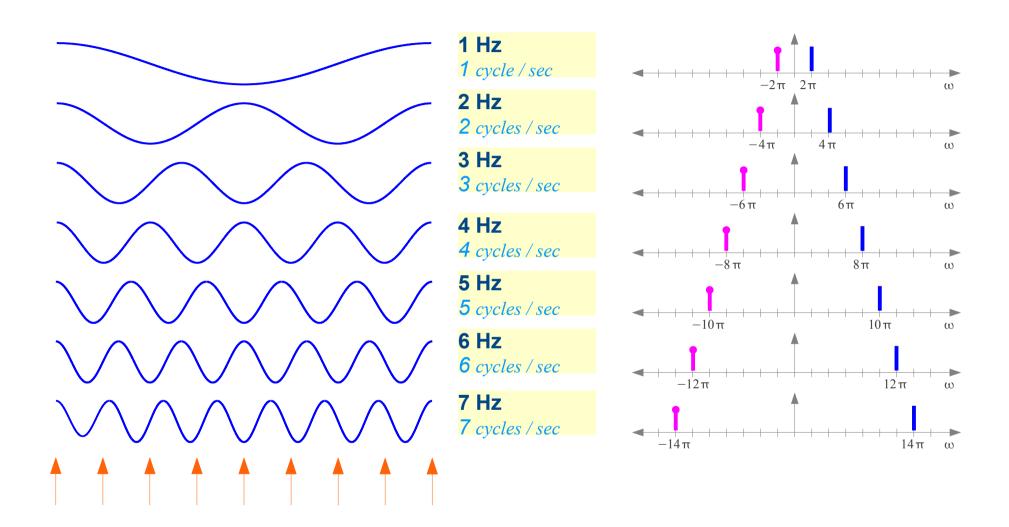


#### **5B Upsampling**

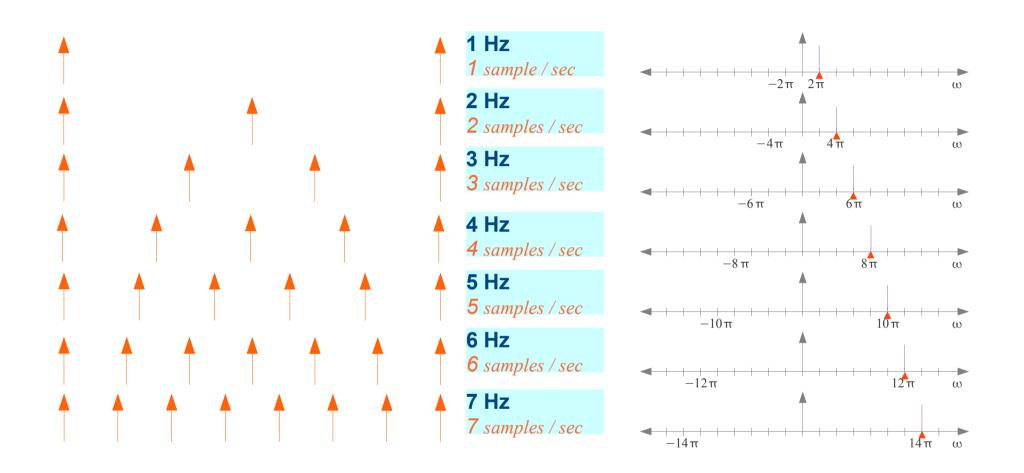
## Signals with Harmonic Frequencies (1)

	<b>1 Hz</b> 1 cycle / sec	$\cos(1 \cdot 2\pi t) = \frac{e^{+j(1 \cdot 2\pi)t} + e^{-j(1 \cdot 2\pi)t}}{2}$
	2 Hz 2 cycles / sec	$\cos(2 \cdot 2\pi t) = \frac{e^{+j(2 \cdot 2\pi)t} + e^{-j(2 \cdot 2\pi)t}}{2}$
	3 Hz 3 cycles / sec	$\cos(3 \cdot 2\pi t) = \frac{e^{+j(3 \cdot 2\pi)t} + e^{-j(3 \cdot 2\pi)t}}{2}$
	<b>4 Hz</b> 4 cycles / sec	$\cos(4\cdot 2\pi t) = \frac{e^{+j(4\cdot 2\pi)t} + e^{-j(4\cdot 2\pi)t}}{2}$
	5 Hz 5 cycles / sec	$\cos(5 \cdot 2\pi t) = \frac{e^{+j(5 \cdot 2\pi)t} + e^{-j(5 \cdot 2\pi)t}}{2}$
	6 Hz 6 cycles / sec	$\cos(6 \cdot 2\pi t) = \frac{e^{+j(6 \cdot 2\pi)t} + e^{-j(6 \cdot 2\pi)t}}{2}$
	7 Hz 7 cycles / sec	$\cos(7 \cdot 2\pi t) = \frac{e^{+j(7 \cdot 2\pi)t} + e^{-j(7 \cdot 2\pi)t}}{2}$
$\uparrow \uparrow \uparrow$		

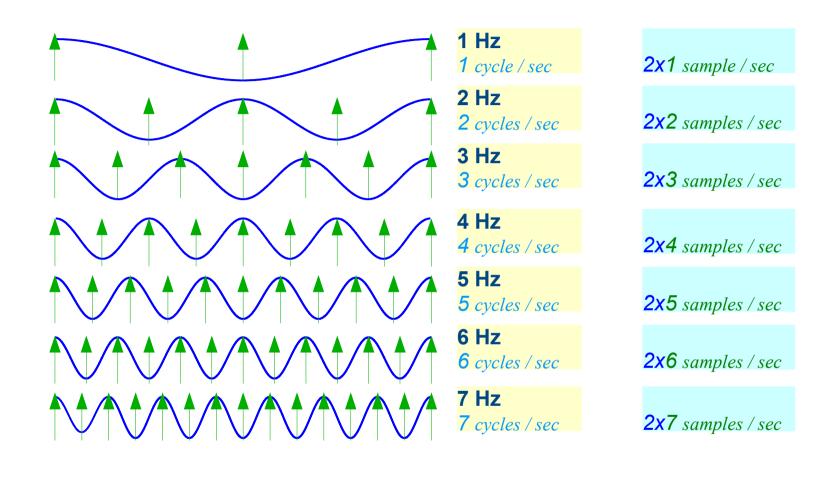
# Signals with Harmonic Frequencies (2)



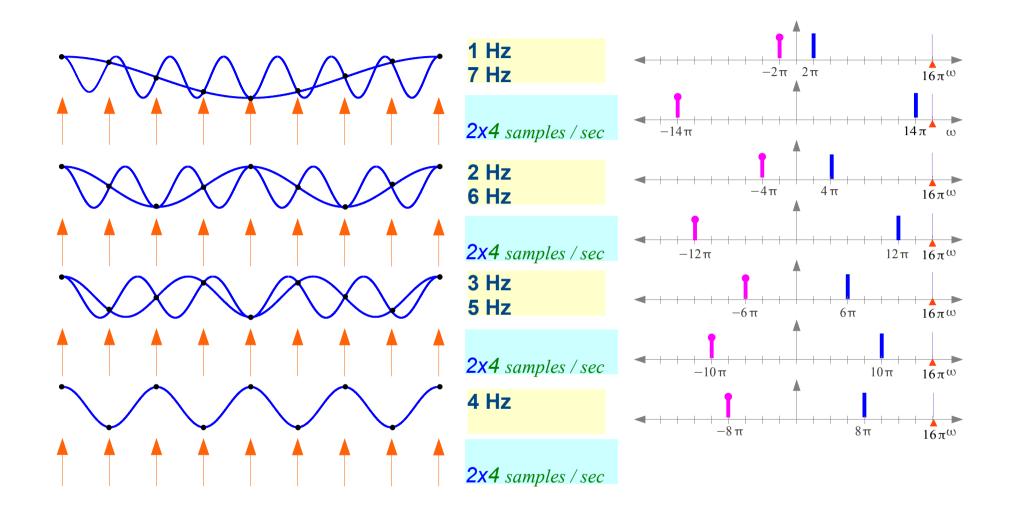
### Sampling Frequency



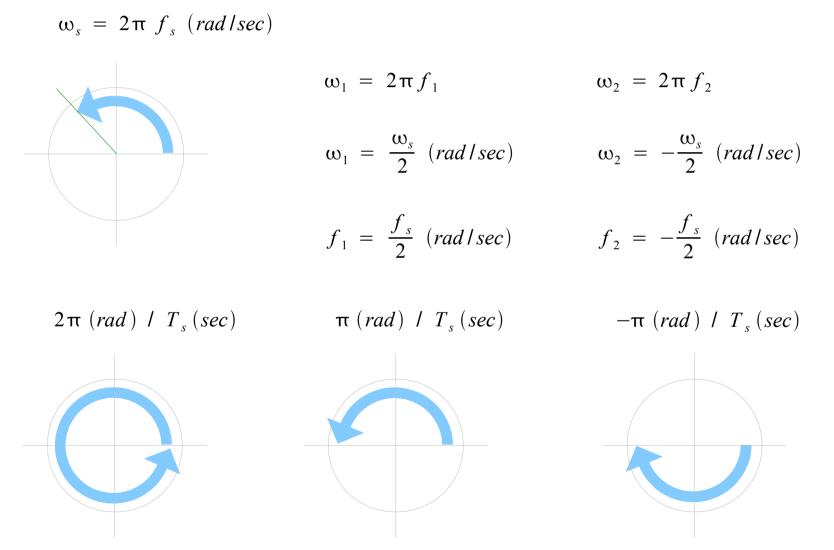
## Nyquist Frequency



# Aliasing

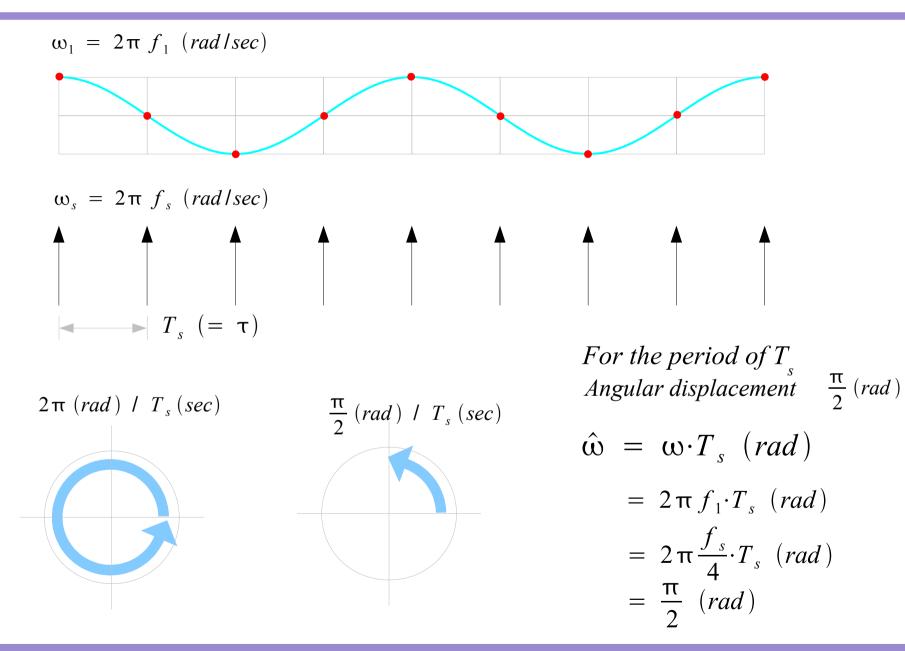


### Sampling



**5B Upsampling** 

# Sampling



### Angular Frequencies in Sampling

continuous-time signals

Signal Frequency

$$f_0 = \frac{1}{T_0}$$

Signal Angular Frequency

$$\omega_0 = 2\pi f_0 (rad/sec)$$

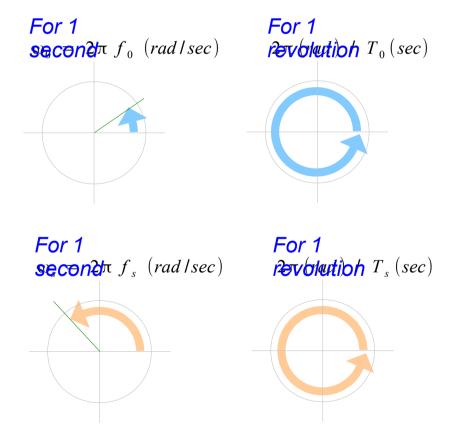
sampling sequence

Sampling Frequency

$$f_s = \frac{1}{T_s}$$

Sampling Angular Frequency

$$\omega_s = 2\pi f_s (rad lsec)$$



#### References

- [1] http://en.wikipedia.org/
- [2] J.H. McClellan, et al., Signal Processing First, Pearson Prentice Hall, 2003
- [3] A "graphical interpretation" of the DFT and FFT, by Steve Mann