Elementary Matrix

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Gauss-Jordan Elimination

Forward Phase - Gaussian Elimination

$$\begin{bmatrix} +2 & +1 & -1 & +8 \\ -3 & -1 & +2 & -11 \\ -2 & +1 & +2 & -3 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ -3 & -1 & +2 & -11 \\ -2 & +1 & +2 & -3 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1/2 & +1/2 & +1 \\ 0 & +2 & +1 & +5 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & +2 & +1 & +5 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & -1 & +1 \end{bmatrix} \longrightarrow \begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & -1/2 & -1/2 &$$

Backward Phase

$$\begin{bmatrix} +1 & +1/2 & -1/2 & +4 \\ 0 & +1 & +1 & +2 \\ 0 & 0 & +1 & -1 \end{bmatrix} \rightarrow \begin{bmatrix} +1 & +1/2 & 0 & +7/2 \\ 0 & +1 & 0 & +3 \\ 0 & 0 & +1 & -1 \end{bmatrix} \rightarrow \begin{bmatrix} +1 & 0 & 0 & +2 \\ 0 & +1 & 0 & +3 \\ 0 & 0 & +1 & -1 \end{bmatrix}$$

Elementary Row Operation

Interchange two rows



Multiply a row by a nonzero constant



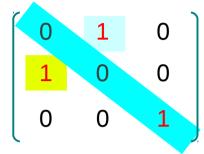
Add a multiple of one row to another



Elementary Matrix

Interchange two rows **Identity Matrix** 0 0 Multiply a row by a nonzero constant $\times C$ Add a multiple of one row to another $\times C$

Multiplication by an Elementary Matrix



4	5	6
1	2	3
7	8	9

Pulse

Pulse

References

- [1] http://en.wikipedia.org/
- [2] Anton & Busby, "Contemporary Linear Algebra"