## Idea (1A)

- Communication Scheduling
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## The Butterfly Swap Operations

$$
\begin{aligned}
& x_{0}^{\prime}=x_{0}+\omega^{k} x_{1} \\
& x_{1}^{\prime}=x_{0}-\omega^{k} x_{1}
\end{aligned}
$$



## The Butterfly Time Multiplexed Operations (1)

$$
\begin{aligned}
& x_{0}^{\prime}=x_{0}+\omega^{k} x_{1} \\
& x_{1}^{\prime}=x_{0}-\omega^{k} x_{1} \\
& x_{0}^{\prime}=x_{0}+\omega^{k} x_{1} \\
& x_{0}=x_{0}^{\prime}-\omega^{k} x_{1} \\
& x_{1}^{\prime}=x_{0}-\omega^{k} x_{1} \\
& \Rightarrow x_{1}^{\prime}=x_{0}^{\prime}-\omega^{k} x_{1}-\omega^{k} x_{1} \\
& x_{1}^{\prime}=x_{0}^{\prime}-2 \omega^{k} x_{1}
\end{aligned}
$$

## The Butterfly Time Multiplexed Operations (2)

$$
\begin{aligned}
& \left\{\begin{array}{l}
x_{0}^{\prime}=x_{0}+\omega^{k} x_{1} \\
x_{1}^{\prime}=x_{0}-\omega^{k} x_{1} \\
x_{1}^{\prime}=x_{0}-\omega^{k} x_{1} \\
\\
x_{1}=\left(x_{0}-x^{\prime}{ }_{1}\right) \omega^{-k} \\
x_{0}^{\prime}=x_{0}+\omega^{k} x_{1} \\
x_{0}^{\prime}=x_{0}+\omega^{k}\left(x_{0}-x_{1}^{\prime}\right) \omega^{-k} \\
x_{1}^{\prime}=2 x_{0}-x_{1}
\end{array}\right.
\end{aligned}
$$

## Communication Patterns - High BW



To avoid deadlock, there must be lower level communication scheduling overhead?

Unless real duplex communication link $\rightarrow$ Shared Bandwidth

## Communication Patterns - Limited BW

communication computation


## Communication Scheduling - Time Multiplexed

$$
\begin{gathered}
x_{0}^{\prime}= \\
x_{0}+\omega^{k} x_{1}
\end{gathered}
$$



Swapping communication pattern can be avoided

## Communication Latency Hiding (1)



## Communication Latency Hiding (2)



Speed Up?<br>Ratio of Comp time to Comm time?

## References

[1] http://en.wikipedia.org/
[2]

