# Euclidean Vector Space (1A)

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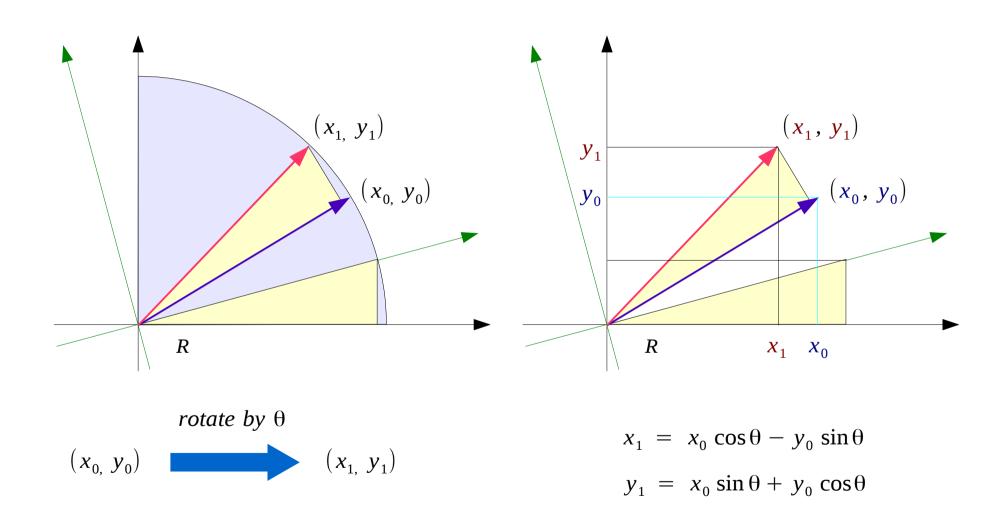
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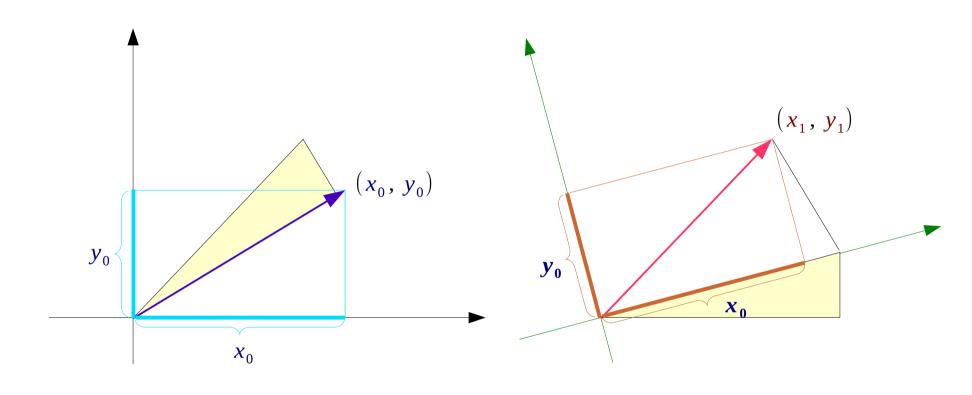
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# Vector Rotation (1)



## Vector Rotation (2)



In the rotated coordinate invariant  $x_0, y_0$ length

Euclidean (1A) Vector Space

# Vector Rotation (3)

 $x_1 = x_0 \cos \theta - y_0 \sin \theta$  $y_1 = x_0 \sin \theta + y_0 \cos \theta$  $(x_1, y_1)$  $(x_1, y_1)$  $\boldsymbol{X}_{\boldsymbol{0}}$  $x_0 \sin \theta$  $(x_0, y_0)$  $(x_0, y_0)$ *y*<sub>1</sub> **y**<sub>0</sub>  $y_0 \cos \theta$ X  $x_0 \sin \theta$  $\boldsymbol{x}_1$  $y_0 \cos \theta$  $y_0 \sin \theta$ 

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#### Normal Vector & 3 Points

<sup>z</sup> Non-collinear 3 points

 $\boldsymbol{a} \times \boldsymbol{b} = \begin{vmatrix} \boldsymbol{i} & \boldsymbol{j} & \boldsymbol{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = \boldsymbol{i} \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} - \boldsymbol{j} \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} + \boldsymbol{k} \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix}$ 

# Normal Vector & 3 Points

<sup>2</sup> Non-collinear 3 points  $\mathcal{Z}$ 

#### References

- [1] http://en.wikipedia.org/
- [2] http://planetmath.org/
- [3] M.L. Boas, "Mathematical Methods in the Physical Sciences"
- [4] D.G. Zill, "Advanced Engineering Mathematics"