Prove that $X U(Y \cap Z)=(X U Y) \cap(X U Z)$

Definition: A set's any collection of elements for which we can always tell whether an element is in the set or not.

Definition: Given two sets $X$ and $Y, X$ union $Y$ is the set of all the elements in $X$ and all the elements in $Y$. We denotes this by XUY.


Definition: Given two sets $X$ and $Y, X$ intersect $Y$ is the set of all the elements that are simultaneously in $X$ and in Y . we denote this by $\mathrm{X} \cap \mathrm{Y}$.


Now to find the left side, we know that X is union to Y intersection Z . This means, that everything is in X and the elements intersecting at X and Y .


On the other right side of the equation, the elements are in the intersection of $X$ union $Y$ and $X$ union to $Z$. If we were to make a diagram of $X$ union $Y$ and another diagram of $X$ union $Z$, we would see that $X$

Union $Y$ is everything in $X$ and $Y$, similarly, $X$ union $Z$ is everything in $X$ and $Z$. If we were to combine these two diagrams together, we see that the diagram looks exactly like the left hand equation, $\mathrm{XU}(\mathrm{Y} \cap \mathrm{Z})$
(XUY)


Z

