

L. *Inventio Curvæ quam Corpus descendens brevissimo tempore describeret ; urgente Vi Centripetâ ad datum punctum tendente, quæ crescat vel decrescat juxta quamvis Potentiam distantia à Centro ; dato nempe imo Curvæ puncto & altitudine in principio Casus. Per Joh. Machin, Astron. Profefs. Gresh. & Reg. Soc. Secret.*

Sit centrum Virium C, (*Fig. 1. 2*), quo centro ad distantiam CB æqualem altitudini unde Corpus casurum est, describatur Circulus BEG, & fiat angulus BCG rectus. Ponatur A punctum Curvæ infimum, ubi axi CB occurrit ad datam distantiam CA. Oportet invenire punctum Q, ubi Curva celerrimi descensus EQA occurrit circulo QF, ad datam aliam distantiam CF. Problema hoc duos habet Casus, quorum alter pendet ab Hyperbola & Circulo, alter ab Ellipsi & Circulo.

Cas. 1. Si fuerit Vis centripeta reciproce ut distantia à Centro. Sit KLM (*Fig. 1.*) Hyperbola quavis reſtanguſa centro C & Aſymptoto CB deſcripta, quæ occurrat normalibus BK, AM ſuper ipſam BC ad puncta B, A erectis, in K & M; ordinatæ vero cuilibet intermedie FL ad punctum F erectæ, in L. Fiat CD ad CG ut \sqrt{AFLM} ad \sqrt{ABKM} , & ſit DH normalis ſuper CG: dein capiatuſ Sector RCB ad Arcam HDCB ut data Area Hyperbolica ABKM ad datum Reſtanguſulum CA \times AM. Tum reſta RC occurret circulo FQ in puncto Q, quod quidem eſt ad Curvam celerrimi deſcenſus EQA.

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Habebitur autem punctum E, à quo inciperet Corporis casus, capiendo Sectorem B C E ad Arcam Quadrantis B C G, in eadem ratione Areæ Hyperbolicæ A B K M ad rectangulum sub C A & A M contentum.

Coroll. Hinc si recta R C, circa centrum C revoluta, faciat Sectores R C B proportionales Areis H D C B, in quibus quadrata Basium C D sumuntur in progressionem Arithmeticâ: tum rectæ C R interfecabunt Curvam E Q A ad distantias à centro C Q, quæ decrescant in progressionem Geometricâ

Cas. 2. Si vero Vis centripeta fuerit reciproce ut alia quævis Potestas distantie à centro; sit $n \neq 1$ Index istius Potestatis (ubi n potest esse Numerus quilibet integer vel fractus, affirmativus vel negativus) sitque $H = C B$ altitudo maxima Curvæ quæsitæ E Q A, $b = C A$ altitudo minima ejusdem, & $A = C F$ altitudo alia quævis intermedia. *Fig. 2.*

In recta C G capiatur C D ad C B ut $\sqrt{b^n}$ ad $\sqrt{H^n}$, atque etiam C H ad C D ut $\sqrt{A^n - b^n}$ ad $\sqrt{H^n - b^n}$. Centro C, semiaxibus C D, C B, describatur Ellipsis B L D, cui occurrat ordinatim applicata H L in puncto L; & ducatur recta L K, quæ Ellipsin tangat in L, & Axi minori C D producto conveniat in K: dein Tangenti K L parallela ducatur N M, circulum B E M G tangens in M & ipsi C D occurrens in N. Denique capiatur Sector R C B, qui sit ad Arcam N M B L K N, inter Circulum & Ellipsin & utriusque Tangentes rectamque N K comprehensam, in ratione Numeri binarii ad Numerum n . Tum recta R C interfecabit Circulum F Q in puncto Q, quod erit ad Curvam celerrimi Defensus E Q A.

Quod si fiat Sector B C E ad aream B D G, inter Ellipseos & Circuli Quadrantes interceptam, in ratione dictâ Binarii ad Numerum n , coeuntibus scilicet punctis L, D & M, G; (ob $A^n = H^n$) erit punctum E unde in-

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choaretur Casus Corporis brevissimo tempore descendens ad A, descensuque suo Curvam EQA describentis, quam tangit recta CE in E, quamque ad angulos rectos secat CB in A.

Harum Constructionum Demonstrationes è Celeberrimi D. *Newtoni Quadraturis*, ejusdemque *Philos. Nat. Principiis* (Prop. XXXIX. & sequentibus aliquibus) petitæ, aliâ datâ occasione ostendentur. Problema autem est alterius generis, Describere Curvas per quas Corpora, de puncto summo E, seu principio casus, demissa, celerissimo descensu ad inferiora data puncta Q, urgente qualibet Vi centripeta, ferrentur; cujus quidem solutio in potestate est. In præsentia sufficiat generalem hujusmodi Curvarum tradidisse Ideam, earumque ad Circuli & Hyperbolæ Quadraturas relationes indicasse, absque quibus easdem Geometricè construere haud adeo proclive est.

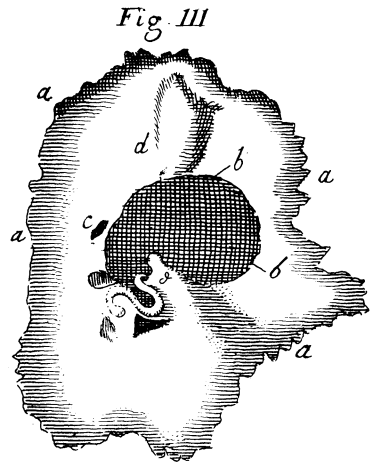
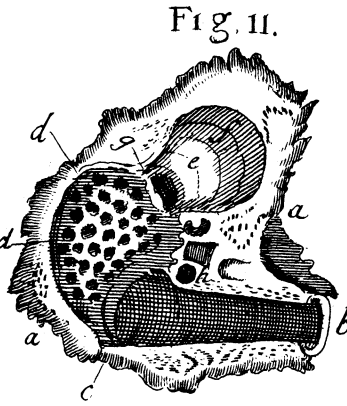
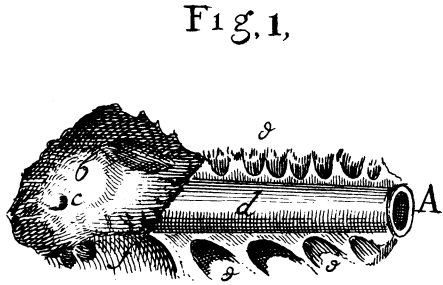


Fig. III

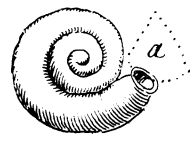
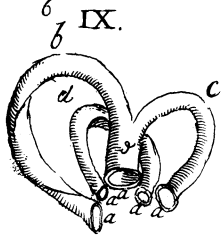
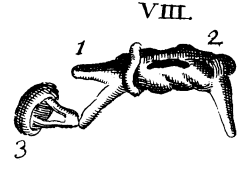
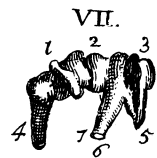


Fig. XI

