## VOLUME OF CONE BY USING INTEGRATION:-



Let us consider a right circular cone of radius $r$ and the height $h$. The volume of cone is obtained by the formula,

$$
V=\int_{a}^{b} \pi y^{2} d x
$$

Here equation of the slant height i.e a straight line passing through origin is given by $y=m x$ and $m=d y / d x$ i.e $m=r / h$

Hence, $y=r x / h$.

$$
\begin{aligned}
& V=\int_{a}^{b} \pi y^{2} d x \\
& V=\pi \int_{0}^{h}(r x / h)^{2} d x \\
& V=\pi r^{2} / h^{2} \int_{0}^{h} x^{2} d x \\
& V=\pi r^{2} / h^{2}\left(x^{3} / 3\right)_{0}^{h} \\
& V=\pi r^{2} / h^{2}\left(h^{3} / 3\right)
\end{aligned}
$$

$$
V=(1 / 3) \pi r^{2} h \text { cubic units. }
$$

